

# Dynamic Memory Allocation

Jinyang Li

based on Tiger Wang's slides

# What we've learnt: how C program is executed by hardware

- Compiler translates C programs to machine code
  - Basic execution:
    - Load instruction from memory, decode + execute, advance %rip
  - Control flow
    - Arithmetic instructions, cmp/test set RFLAGS
    - jge (...) changes %rip depending on RFLAGS
  - Procedure call
    - return address is stored on stack
    - %rsp points to top of stack (stack grows down)
    - call/ret
- Linking:
  - Combine multiple compiled object files together
  - Resolve and relocate symbols (functions, global variables)

# Today's lesson plan

,

- dynamic memory allocation (malloc/free)

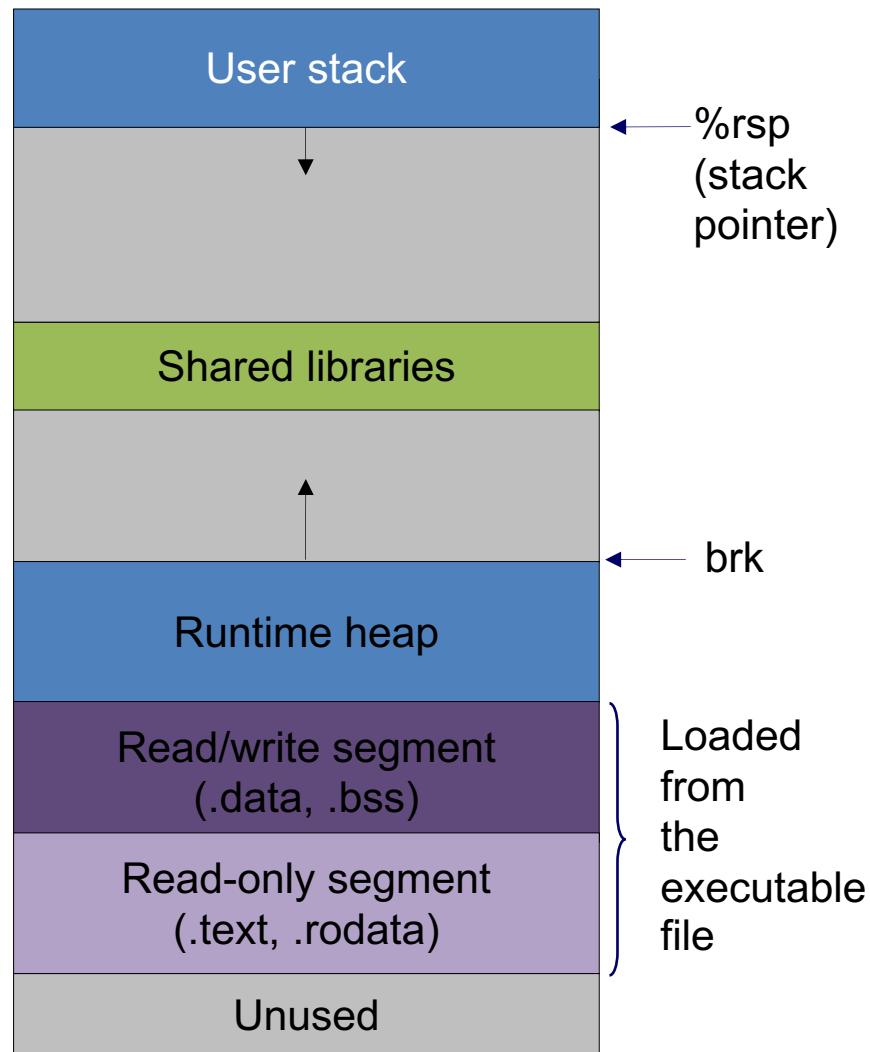
# Why dynamic memory allocation?

```
typedef struct node {  
    int val;  
    struct node *next;  
} node;  
  
void list_insert(node *head, int v)  
{  
    node *np = malloc(sizeof(node));  
    np->next = head;  
    np->val = v;  
    *head = np;  
}  
  
int main(void)  
{  
    char buf[100];  
    node *head = NULL;  
    while (fgets(buf, 100, stdin)) {  
        list_insert(&head, atoi(buf));  
    }  
}
```

How many nodes to allocate is only known at runtime (when the program executes)

# Dynamic allocation on heap

Question: can one dynamically allocate memory on stack?

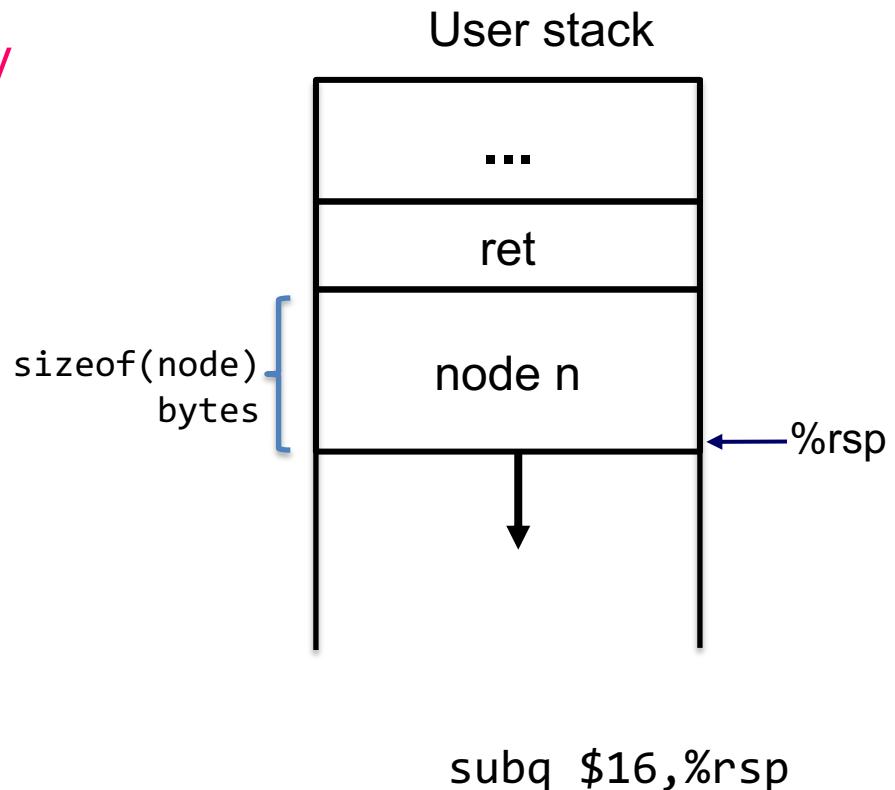


# Dynamic allocation on heap

Question: Is it possible to dynamically allocate memory on stack?

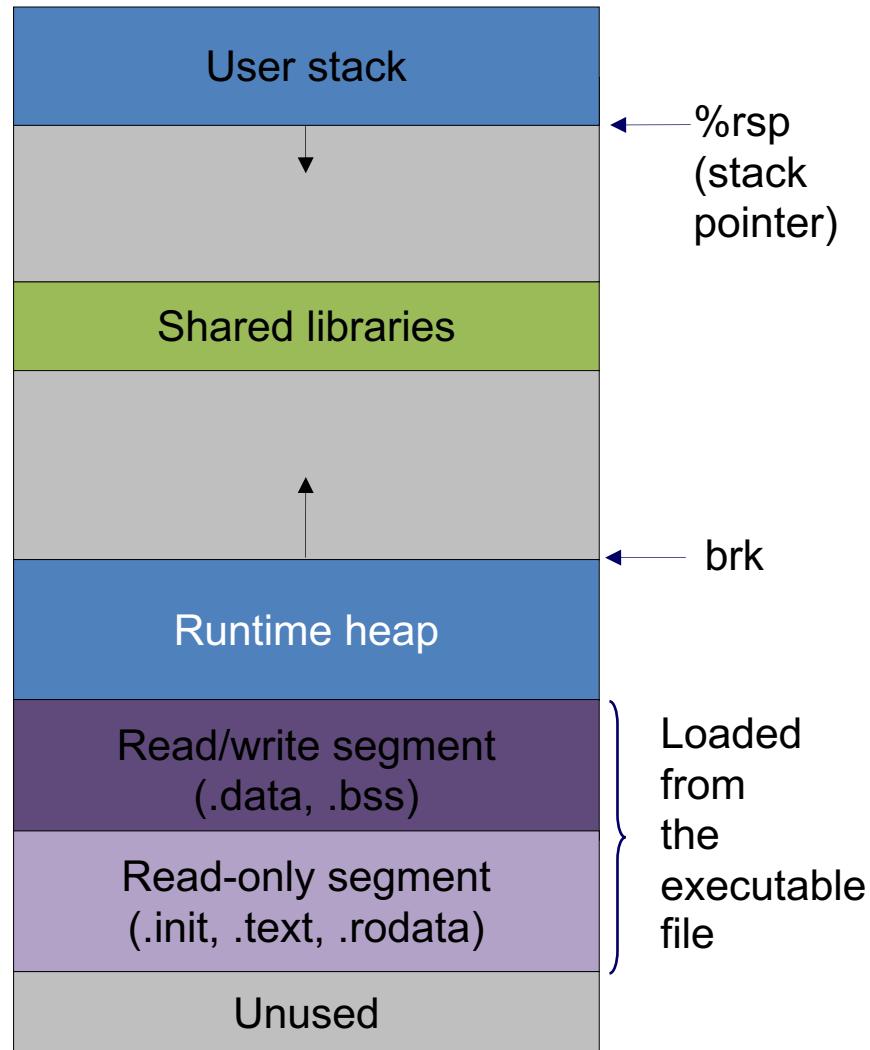
Answer: Yes, but space is freed upon function return

```
void  
list_insert(node *head, int v) {  
    node n;  
    node *np = &n;  
    np->next = head;  
    np->val= v;  
    *head = np;  
}
```



# Dynamic allocation on heap

Question: How to allocate memory on heap?



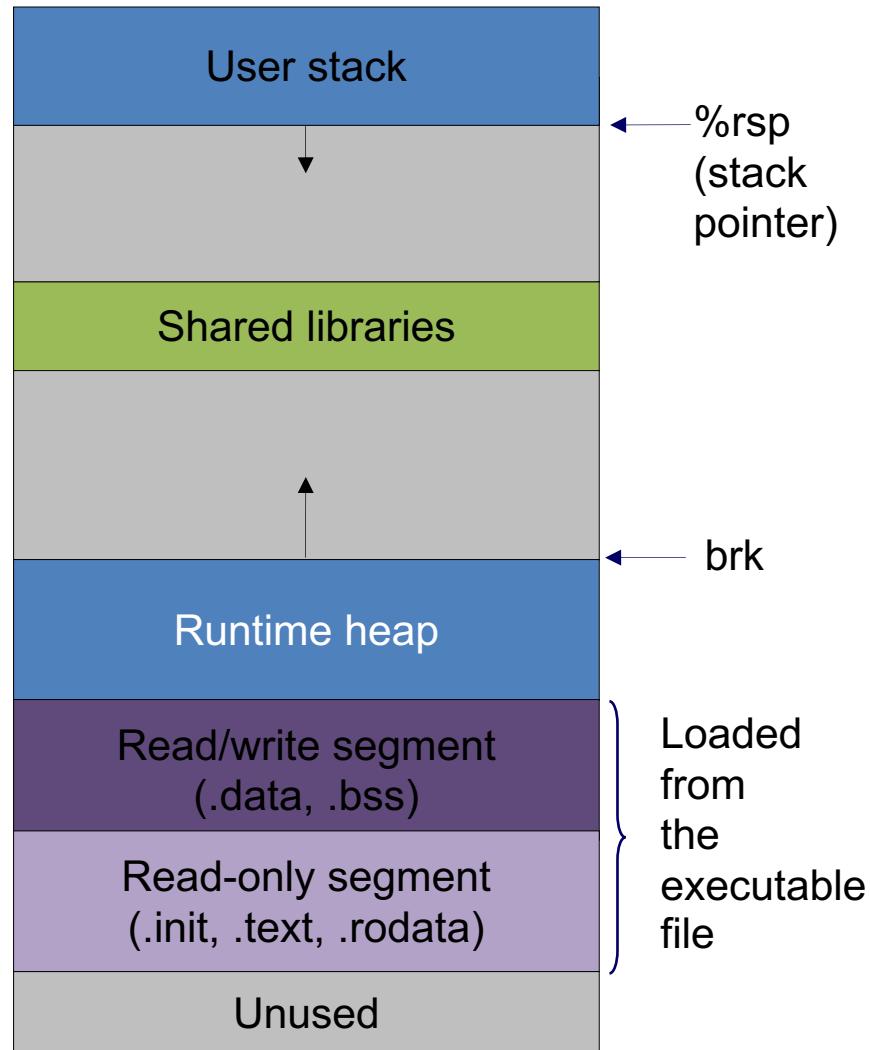
# Dynamic allocation on heap

Question: How to allocate memory on heap?

Ask OS for allocation on the heap via [system calls](#)

```
void *sbrk(intptr_t size);
```

It increases the top of heap by “size” and returns a pointer to the base of new storage. The “size” can be a negative number.



# Dynamic allocation on heap

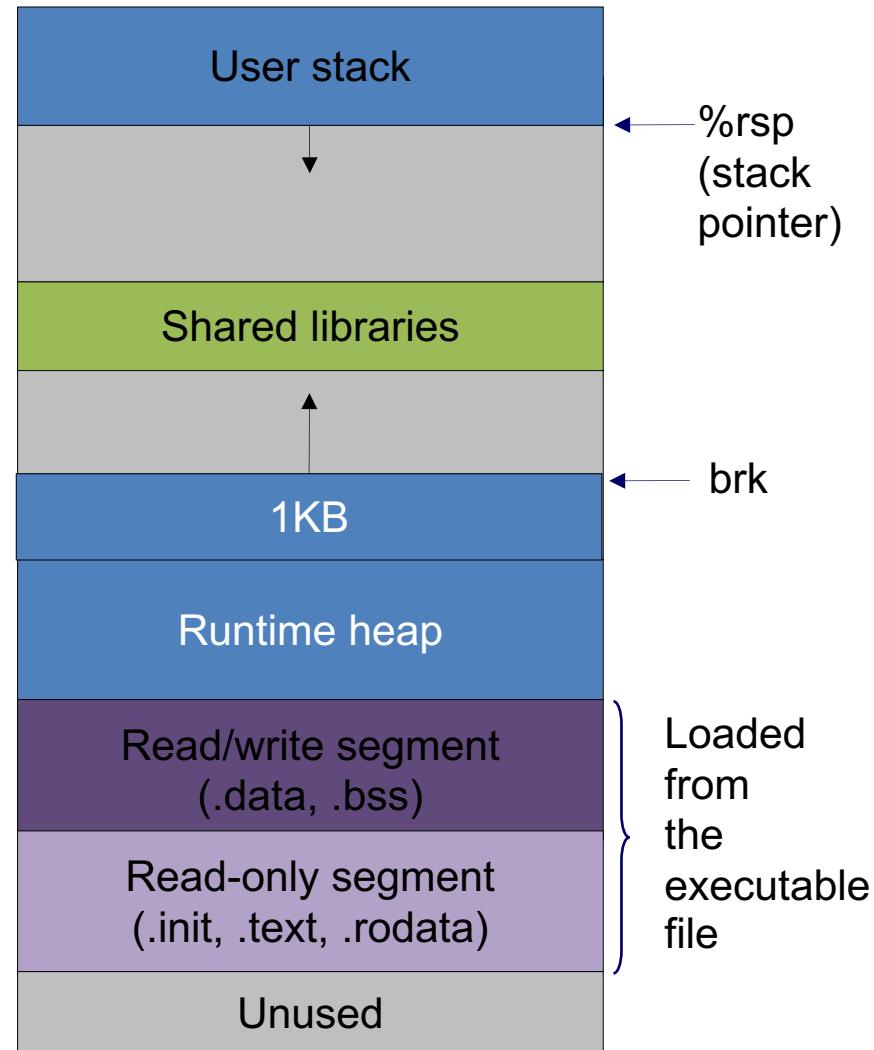
Question: How to allocate memory on heap?

Ask OS for allocation on the heap via [system calls](#)

```
void *sbrk(intptr_t size);
```

It increases the top of heap by “size” and returns a pointer to the base of new storage. The “size” can be a negative number.

```
p = sbrk(1024) //allocate 1KB
```



# Dynamic allocation on heap

Question: How to allocate memory on heap?

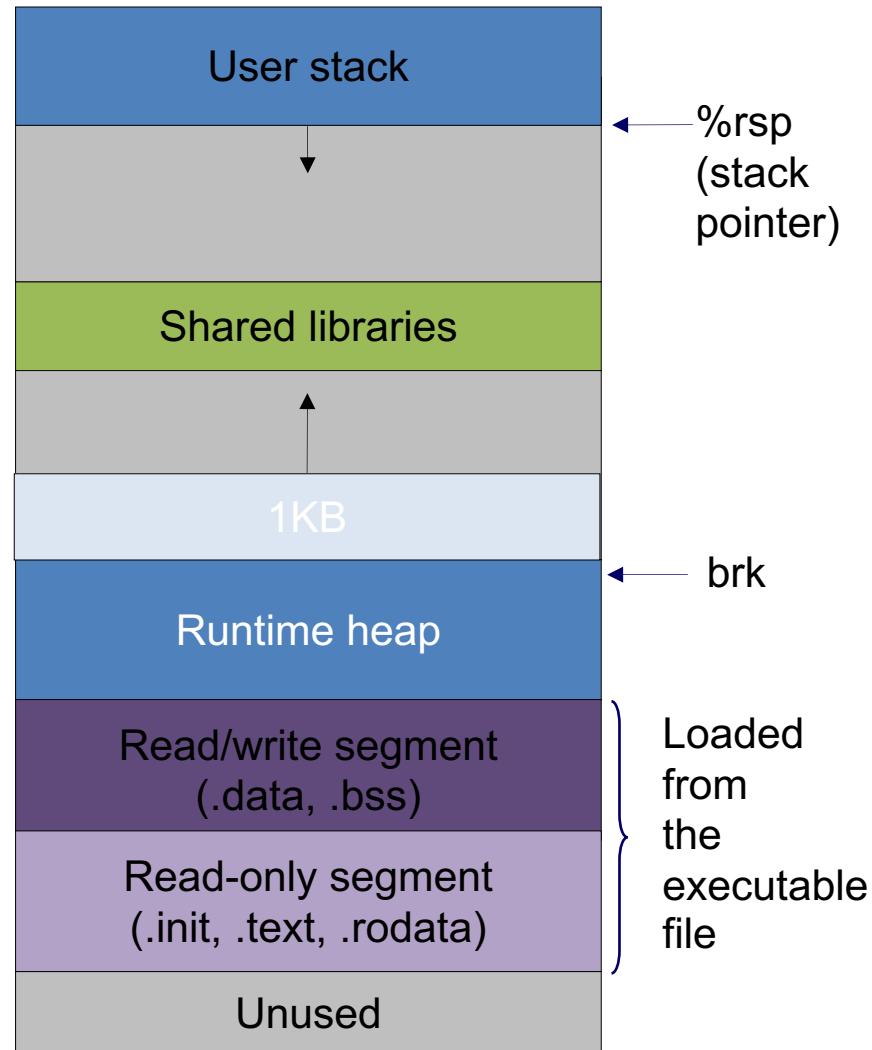
Ask OS for allocation on the heap via [system calls](#)

```
void *sbrk(intptr_t size);
```

It increases the top of heap by “size” and returns a pointer to the base of new storage. The “size” can be a negative number.

```
p = sbrk(1024) //allocate 1KB
```

```
sbrk(-1024) //free p
```



# Dynamic allocation on heap

Question: How to allocate memory on heap?

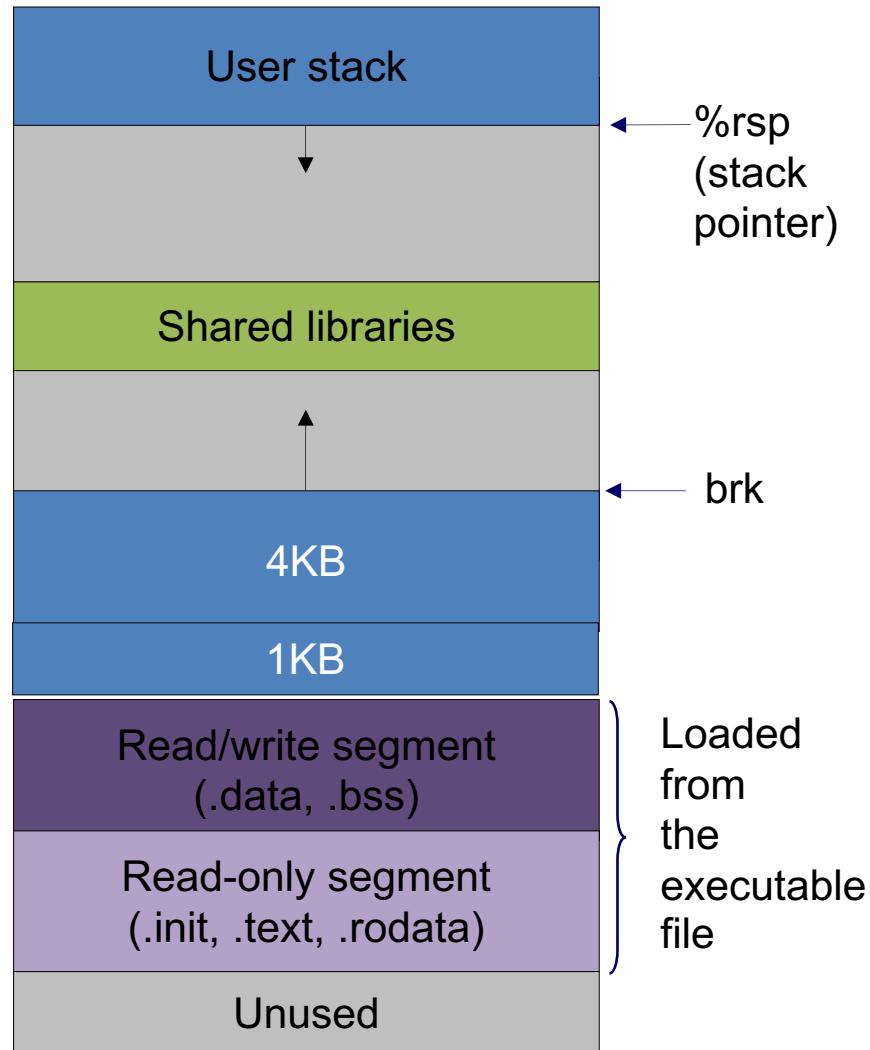
Ask OS for allocation on the heap via [system calls](#)

```
void *sbrk(intptr_t size);
```

Issue I – can only free the memory on the top of heap

```
p1 = sbrk(1024) //allocate 1KB  
p2 = sbrk(4096) //allocate 4KB
```

How to free p1?



# Dynamic allocation on heap

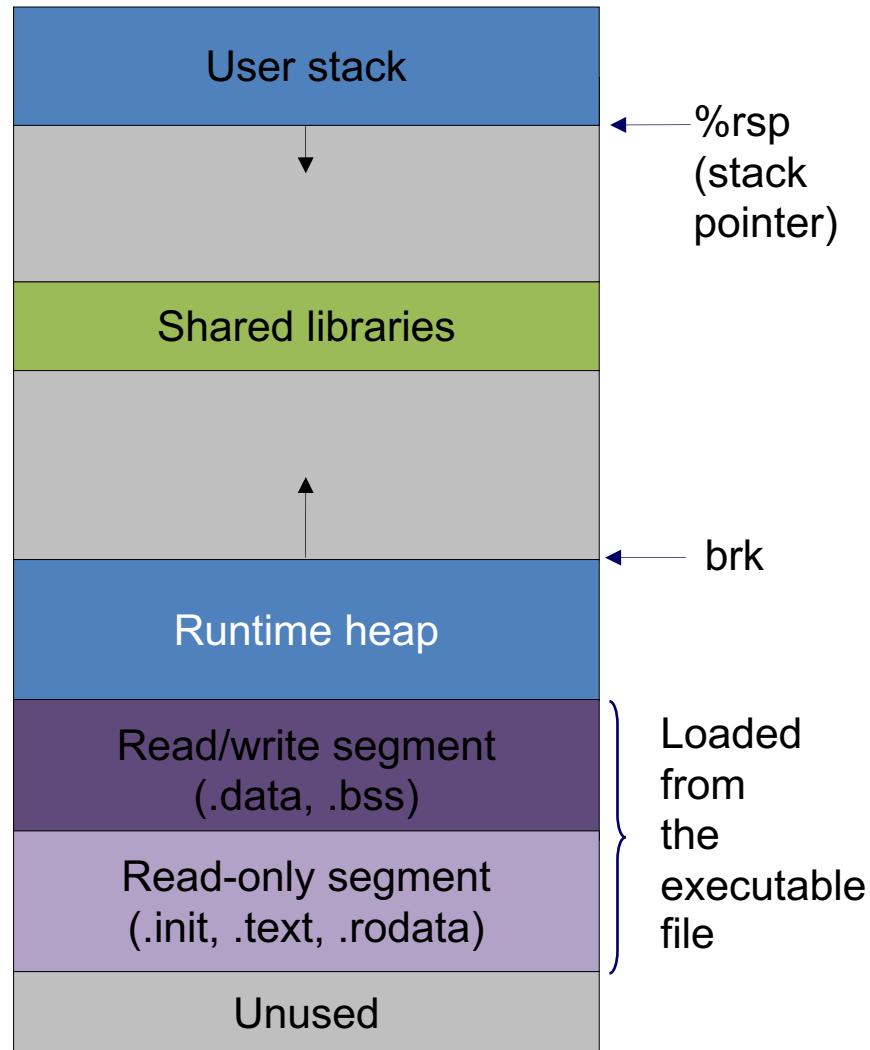
Question: How to allocate memory on heap?

Ask OS for allocation on the heap via [system calls](#)

```
void *sbrk(intptr_t size);
```

Issue I – can only free the memory on the top of heap

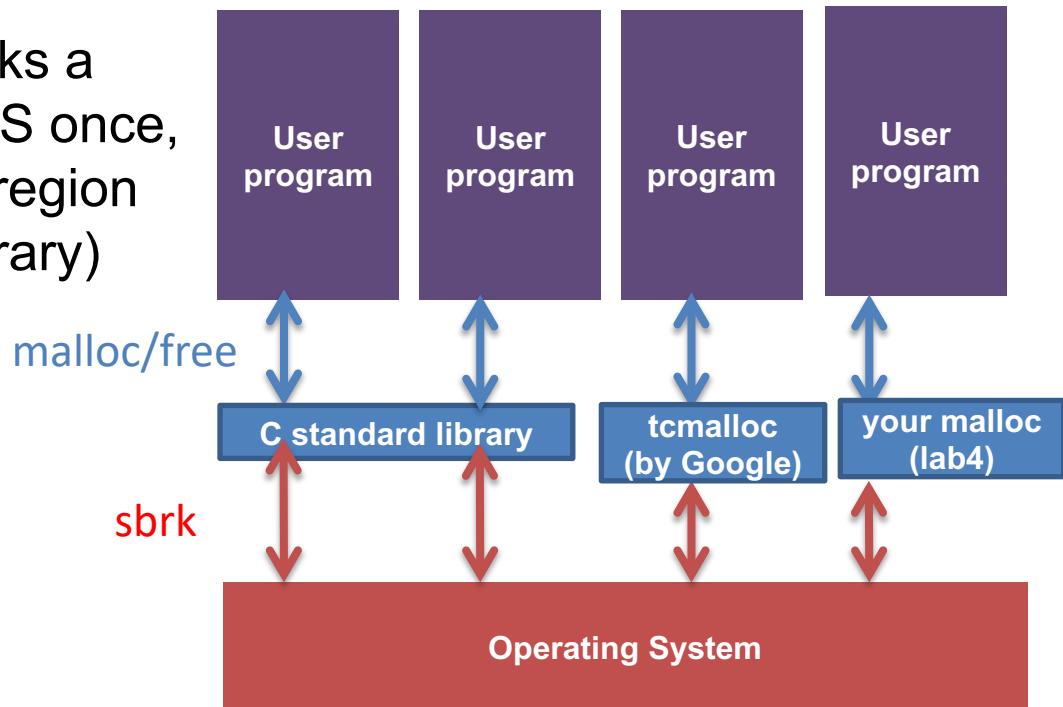
Issue II – system call has high performance cost > 10X



# Dynamic allocation on heap

Question: How to efficiently allocate memory on heap?

Basic idea: user program asks a large memory region from OS once, then manages this memory region by itself (using a “malloc” library)



# How to implement a memory allocator?

- API:
  - `void* malloc(size_t size);`
  - `void free(void *ptr);`
- Goal:
  - Efficiently utilize acquired memory with high throughput
    - high throughput – how many mallocs / frees can be done per second
    - high utilization – fraction of allocated size / total heap size

# How to implement a memory allocator?

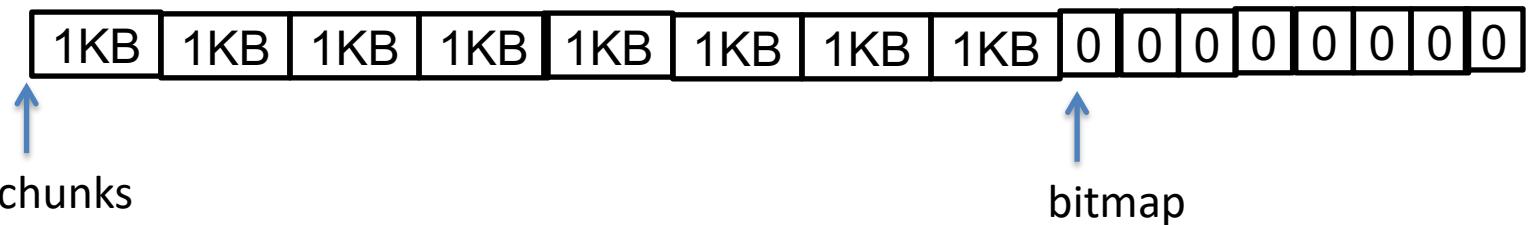
- Assumptions on application behavior:
  - Use APIs correctly
    - Argument of free must be the return value of a previous malloc
    - No double free
  - Use APIs freely
    - Can issue an arbitrary sequence of malloc/free
- Restrictions on the allocator:
  - Once allocated, space cannot be moved around

# Questions

- (Basic book-keeping) How to keep track which bytes are free and which are not?
- (Allocation decision) Which free chunk to allocate?
- (API restriction) free is only given a pointer, how to find out the allocated chunk size?

# How to bookkeep? Strawman #1

- Structure heap as n 1KB chunks + n metadata

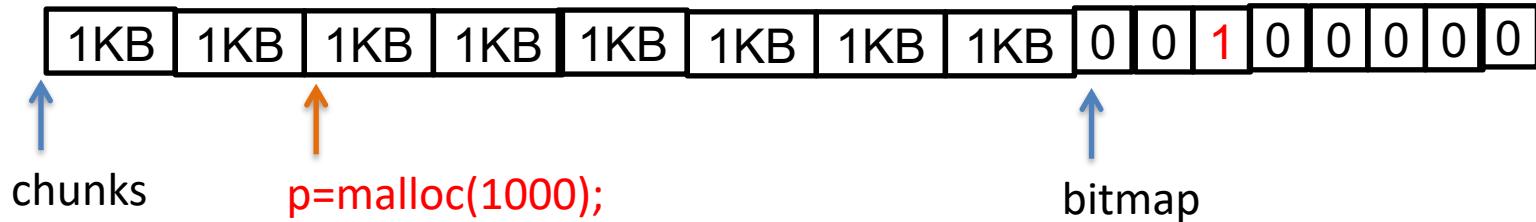


```
#define CHUNKSIZE 1<<10;
typedef char[CHUNKSIZE] chunk;
char *bitmap;
chunk *chunks;
size_t n_chunks;

void init() {
    n_chunks = 128;
    sbrk(n_chunks*sizeof(chunk)+ n_chunks/8);
    chunks = (chunk *)heap_lo();
    bitmap = heap_lo() + n_chunks *CHUNKSIZE;
}
```

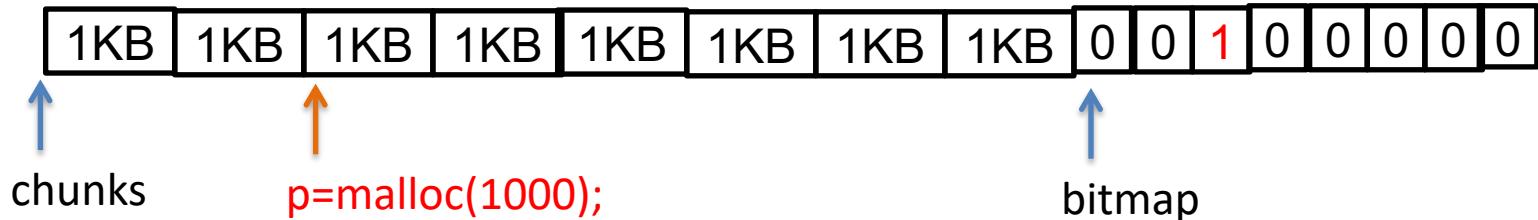
Assume allocator asks for enough memory from OS in the beginning

# How to bookkeep? Strawman #1



```
void* malloc(size_t sz) {  
    // find out # of chunks needed to fit sz bytes  
    CSZ = ...  
  
    //find csz consecutive free chunks according to bitmap  
    int i = find_consecutive_chunks(bitmap);  
  
    // return NULL if did not find csz free consecutive chunks  
    if (i < 0)  
        return NULL;  
  
    // set bitmap at positions i, i+1, ... i+csz-1  
    bitmap_set_pos(bitmap, i, csz);  
    return (void *)&chunks[i];  
}
```

# How to bookkeep? Strawman #1



```
void free(void *p) {  
    i = ((char *)p - (char *)chunks)/sizeof(chunk);  
    bitmap_clear_pos(bitmap, i); //how many bits to clear??  
}
```

- Problem with strawman?
  - free does not know how many chunks allocated
  - wasted space within a chunk (internal fragmentation)
  - wasted space for non-consecutive chunks (external fragmentation)

# How to bookkeep? Other Strawmans

- How to support a variable number of variable-sized chunks?
  - Idea #1: use a hash table to map address → [chunk size, status]
  - Idea #2: use a linked list in which each node stores [address, chunk size, status] information.

## Problems of strawmans?

Implementing a hash table and linked list requires use of a dynamic memory allocator!

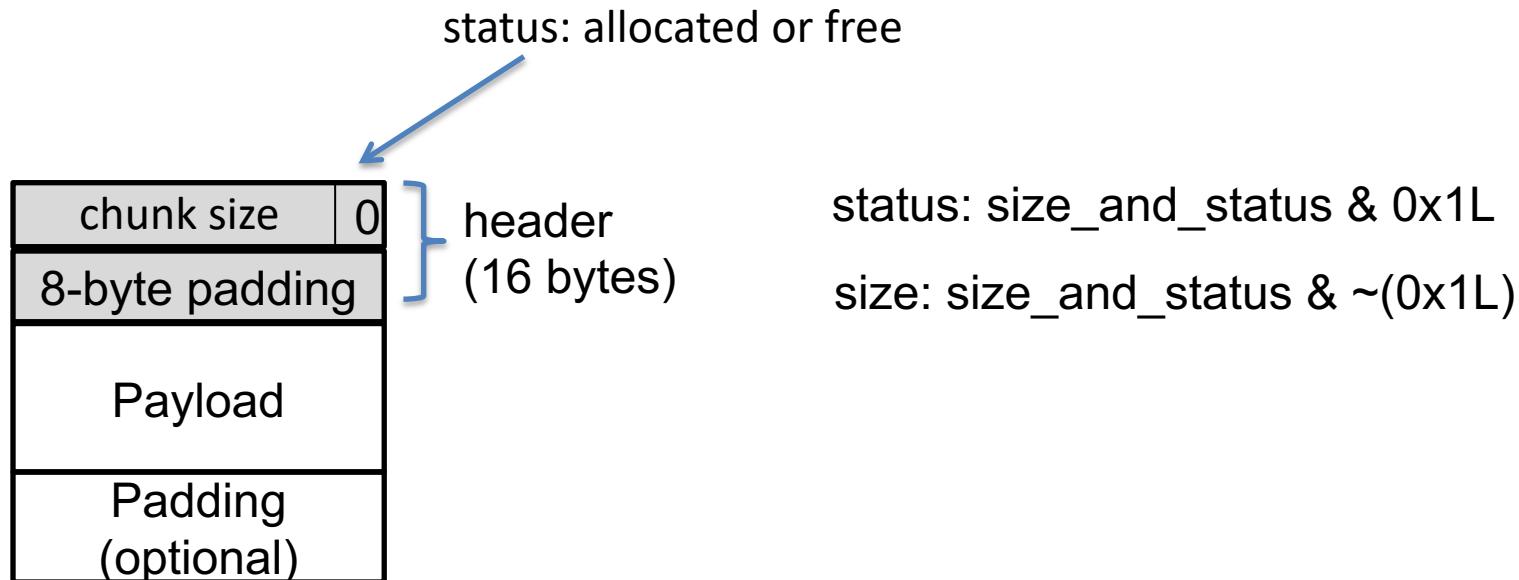
# Today's lesson plan

- Previously:
  - Why dynamic memory allocation?
  - Design requirements and challenges
- Today:
  - Implicit list
  - Explicit list

**How to implement a  
“linked list” without use of malloc**

# Implicit list

- Embed chunk metadata in the chunks
  - Chunk has a header storing size and status
  - 16-byte aligned
    - Payload starting address must be some multiple of 16
    - To simplify design, make header size 16 byte, payload size  $x * 16$  bytes

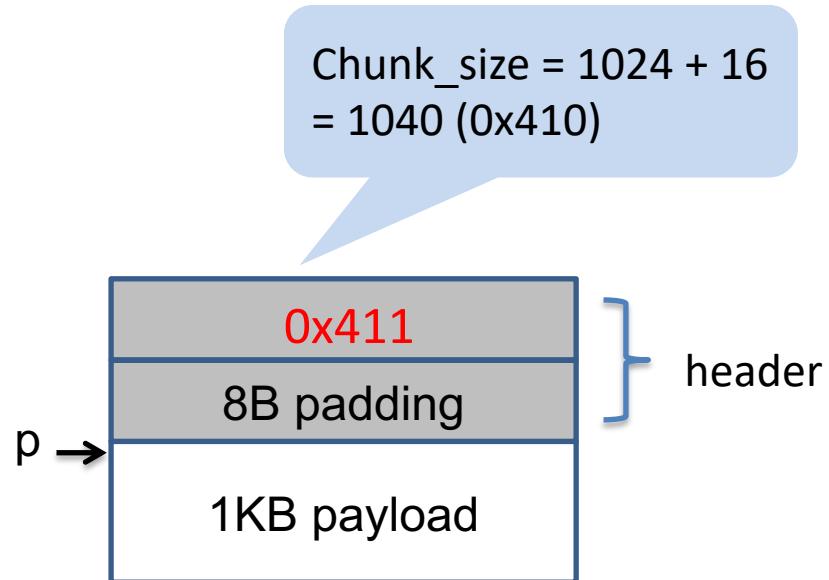


# Implicit list

Embed chunk metadata in the chunks

- Chunk has a header storing size and status
- Payload is 16-byte aligned

```
p = malloc(1024)
```

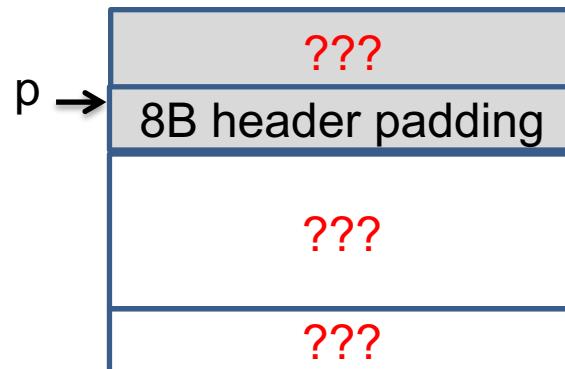


# Implicit list

Embed chunk metadata in the chunks

- Chunk has a header storing size and status
- Payload is 16-byte aligned

```
p = malloc(1)
```

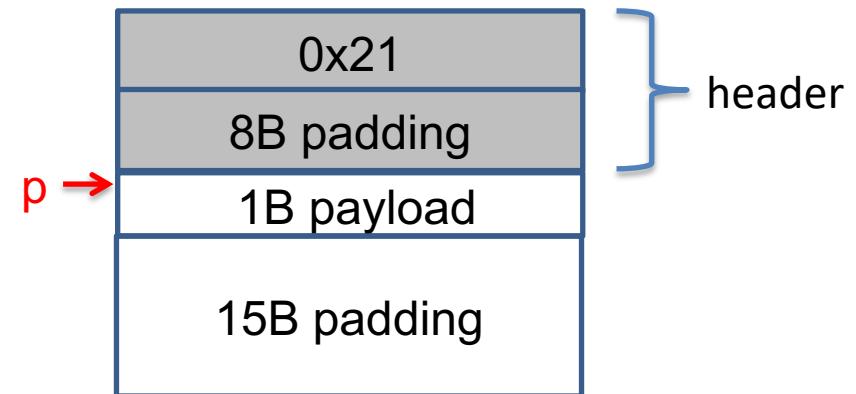


# Implicit list

Embed chunk metadata in the chunks

- Chunk has a header storing size and status
- Payload is 16-byte aligned

```
p = malloc(1)
```



# How to initialize an implicit list

```
typedef struct {
    unsigned long size_and_status;
    unsigned long padding;
} header;

void init_chunk(header *p, unsigned long sz, bool status)
{
    p->size_and_status = sz | (unsigned long) status;
}

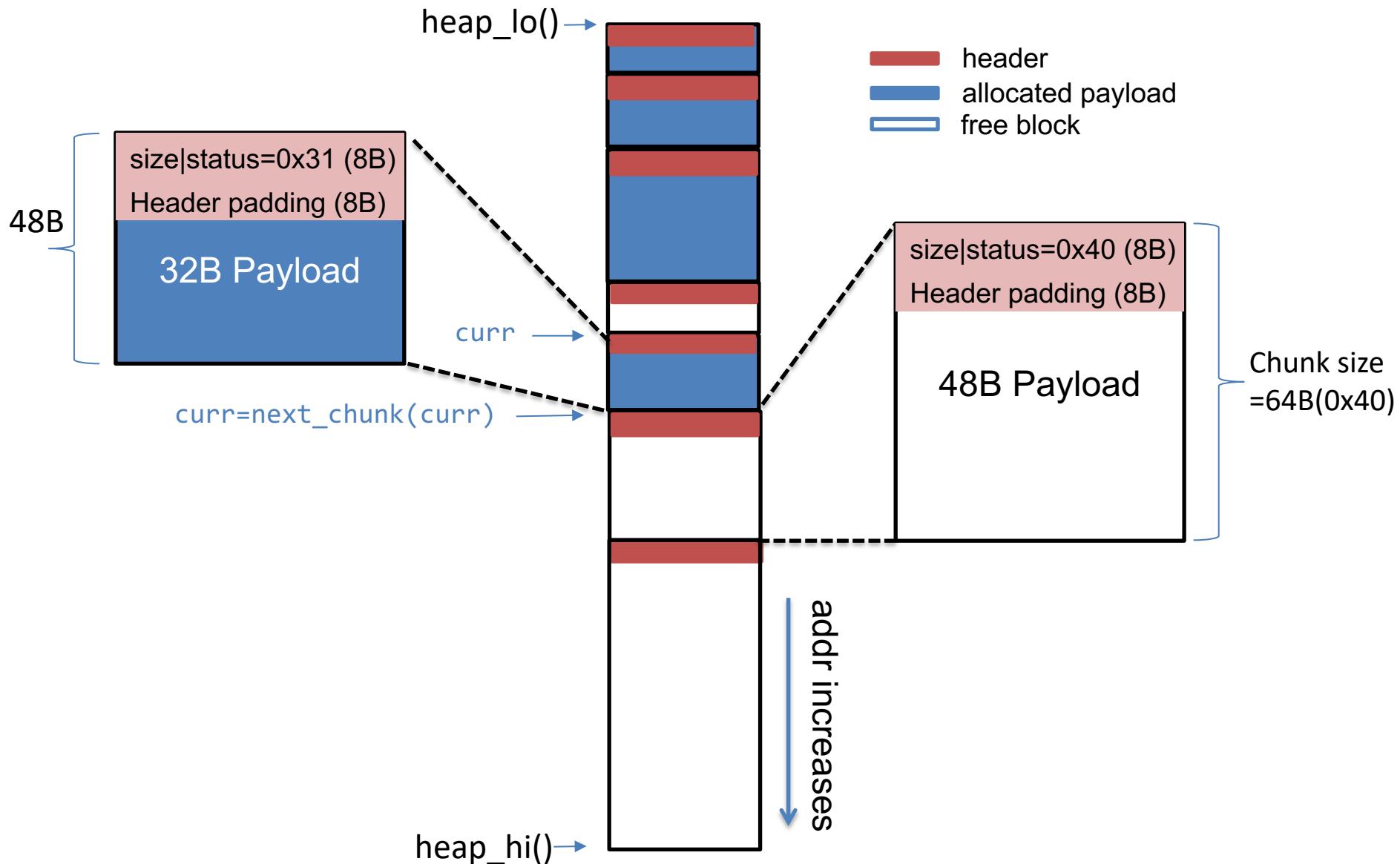
void init()
{
    header *p;
    p = ask_os_for_chunk(INITIAL_CSZ);
    init_chunk(p, INITIAL_CSZ, status);
}
```

# How to traverse an implicit list

```
bool get_status(header *h) {  
    // return status of the chunk  
}  
size_t get_size(header *h) {  
    // return size of the chunk  
}  
  
header *next_chunk(header *curr) {  
    // How to set curr to point to next chunk?  
}  
  
void traverse_implicit_list() {  
    header *curr = (header *)heap_lo();  
    while ((char *)curr < heap_high()) {  
        bool allocated = get_status(curr);  
        size_t csz = get_chunksz(curr);  
        printf("chunk size=%d status=%d\n", csz, allocated);  
        curr = next_chunk(curr);  
    }  
}
```

```
typedef struct {  
    unsigned long size_and_status;  
    unsigned long padding;  
} header;
```

# How to traverse an implicit list

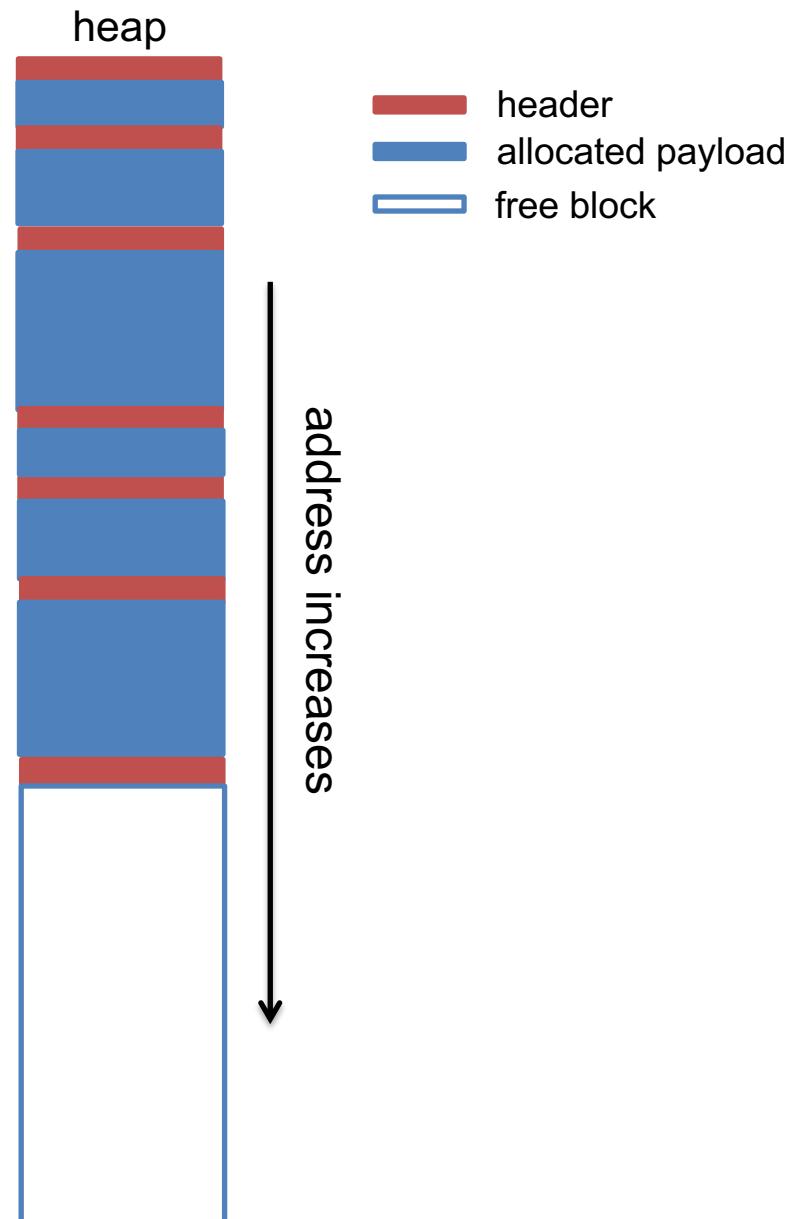


# malloc() in an implicit list

```
void malloc(unsigned long size) {  
    unsigned long chunk_sz = align(size) + sizeof(header);  
    header *h = find_fit(chunk_sz);  
    //split if chunk is larger than necessary  
    split(h, chunk_sz);  
    set_status(h, true);  
}
```

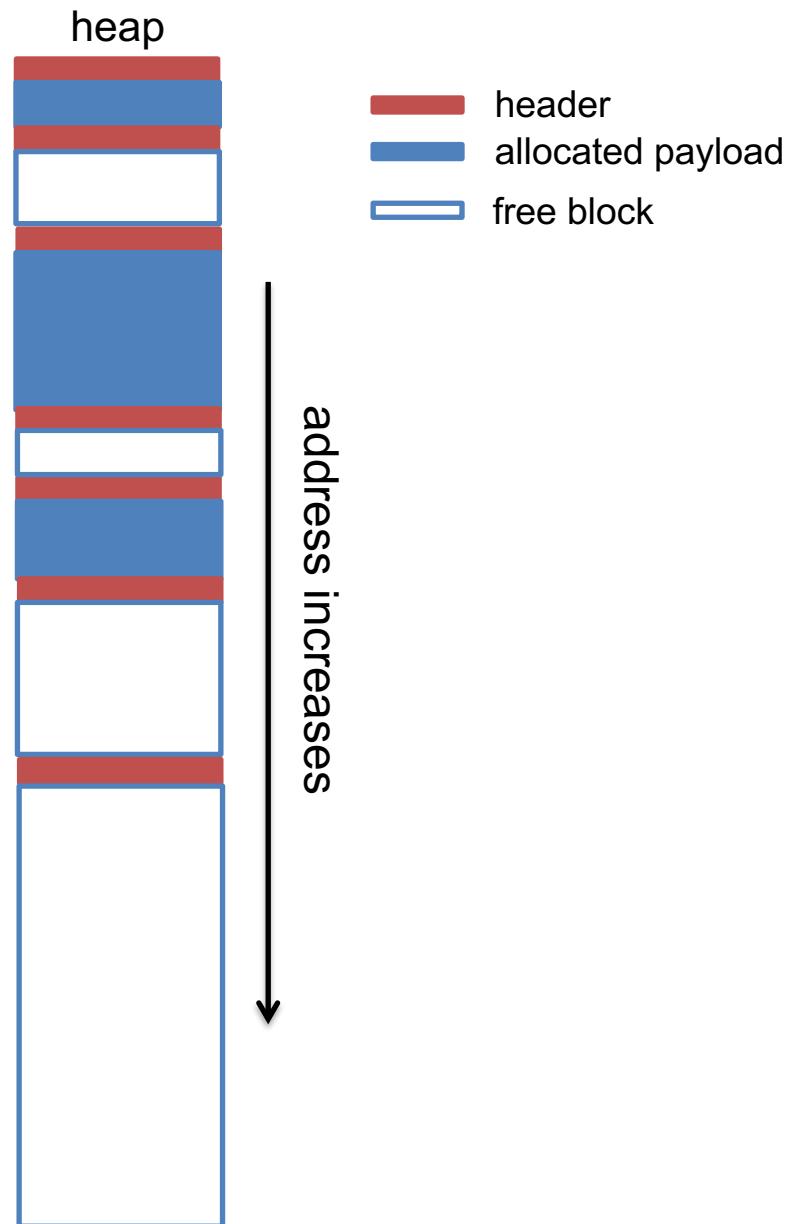
# Where to place an allocation?

```
p1 = malloc(8)
p2 = malloc(24)
p3 = malloc(56)
p4 = malloc(8)
p5 = malloc(24)
p6 = malloc(56)
```



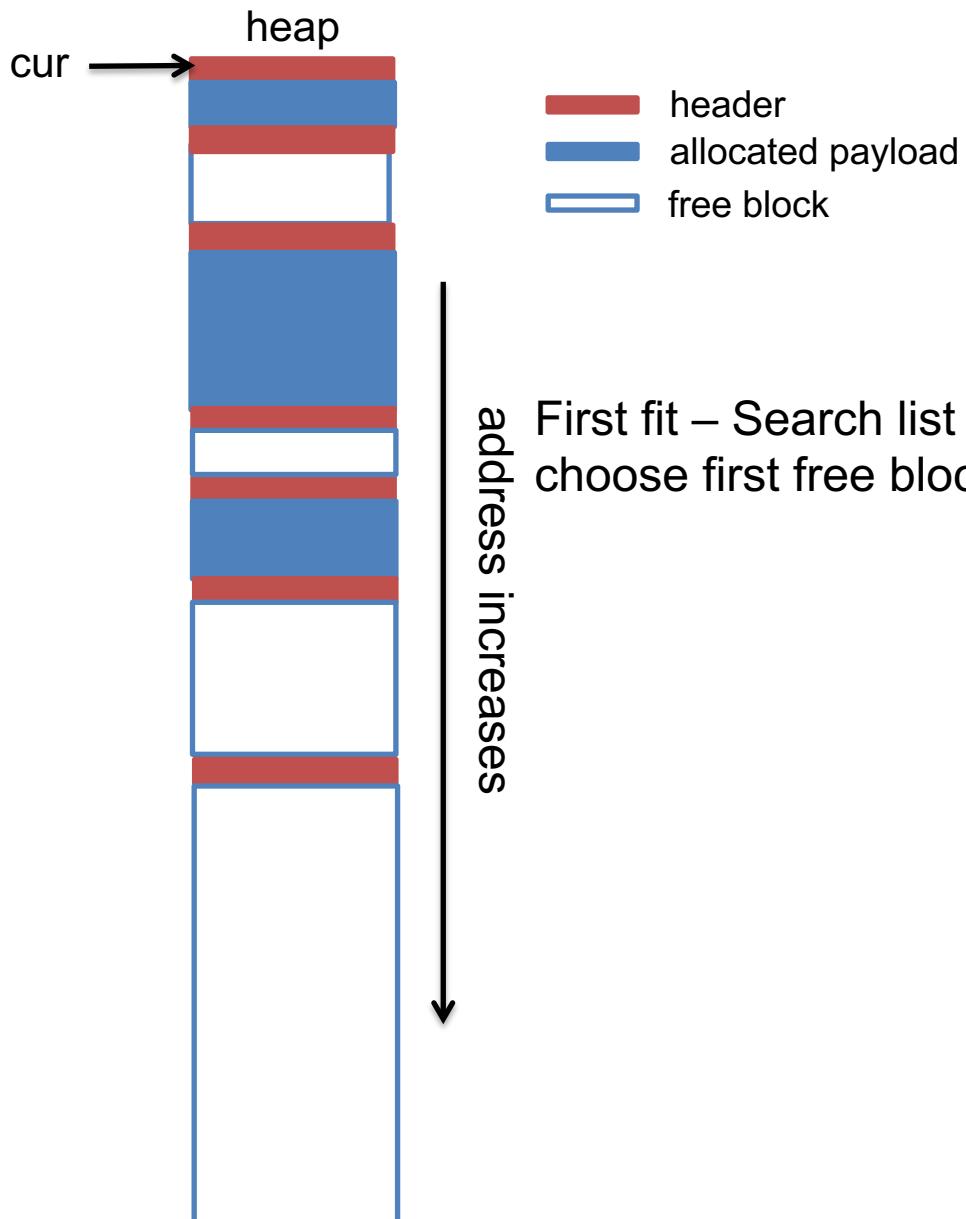
# Where to place an allocation?

```
p1 = malloc(8)
p2 = malloc(24)
p3 = malloc(56)
p4 = malloc(8)
p5 = malloc(24)
p6 = malloc(56)
free(p2)
free(p4)
free(p6)
```



# First fit

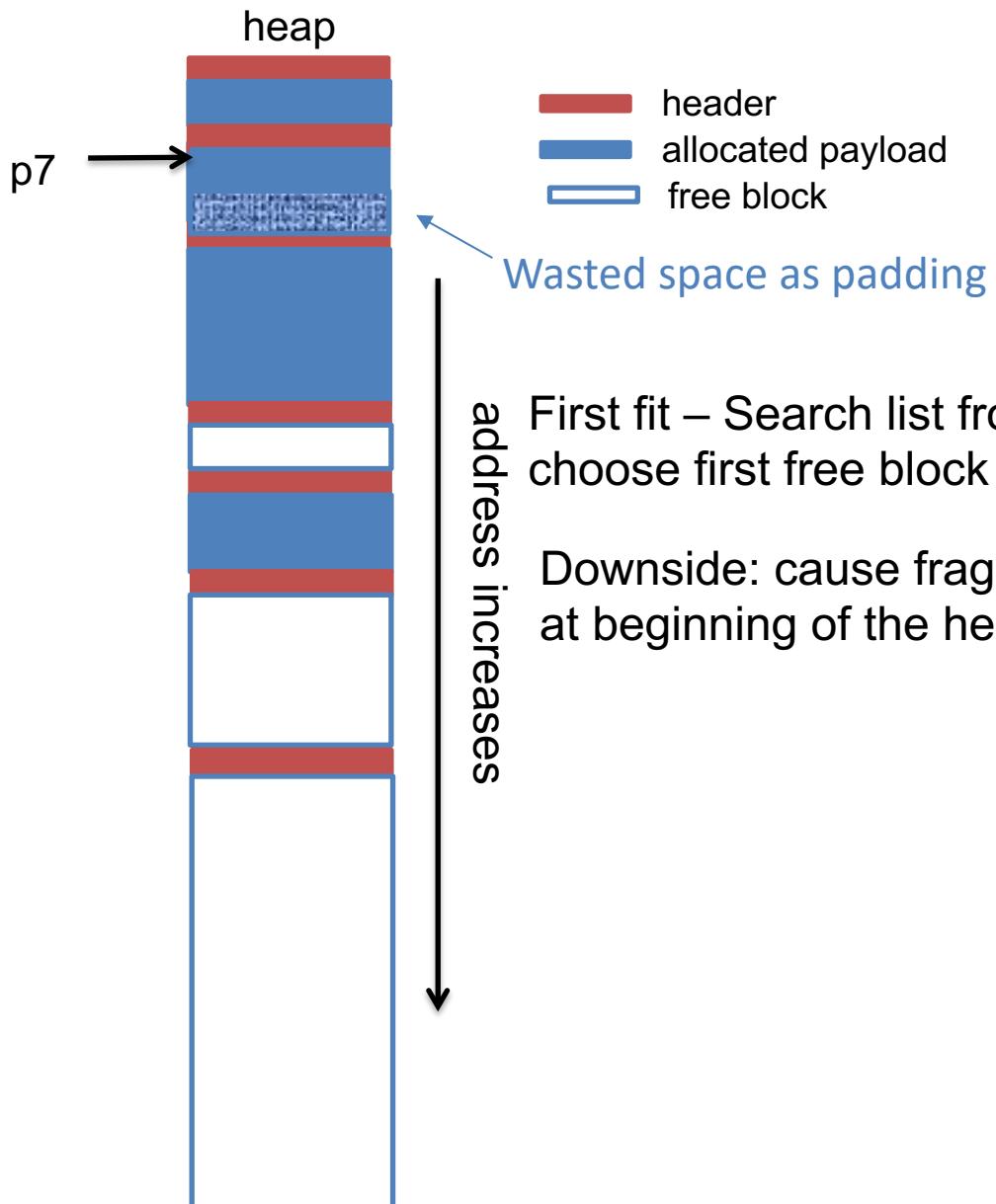
```
p1 = malloc(8)
p2 = malloc(24)
p3 = malloc(56)
p4 = malloc(8)
p5 = malloc(24)
p6 = malloc(56)
free(p2)
free(p4)
free(p6)
p7 = malloc(8)
```



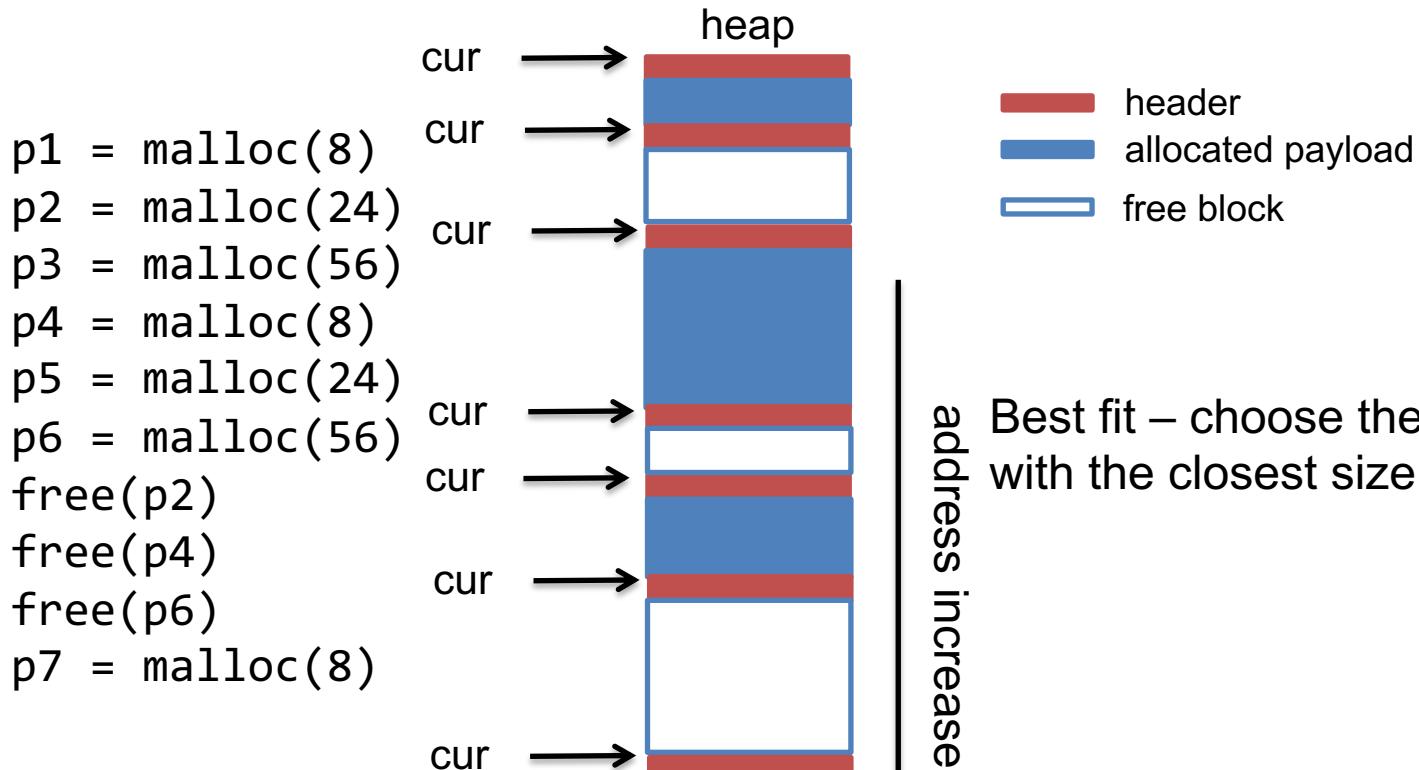
First fit – Search list from beginning,  
choose first free block that fits

# First fit

```
p1 = malloc(8)
p2 = malloc(24)
p3 = malloc(56)
p4 = malloc(8)
p5 = malloc(24)
p6 = malloc(56)
free(p2)
free(p4)
free(p6)
p7 = malloc(8)
```



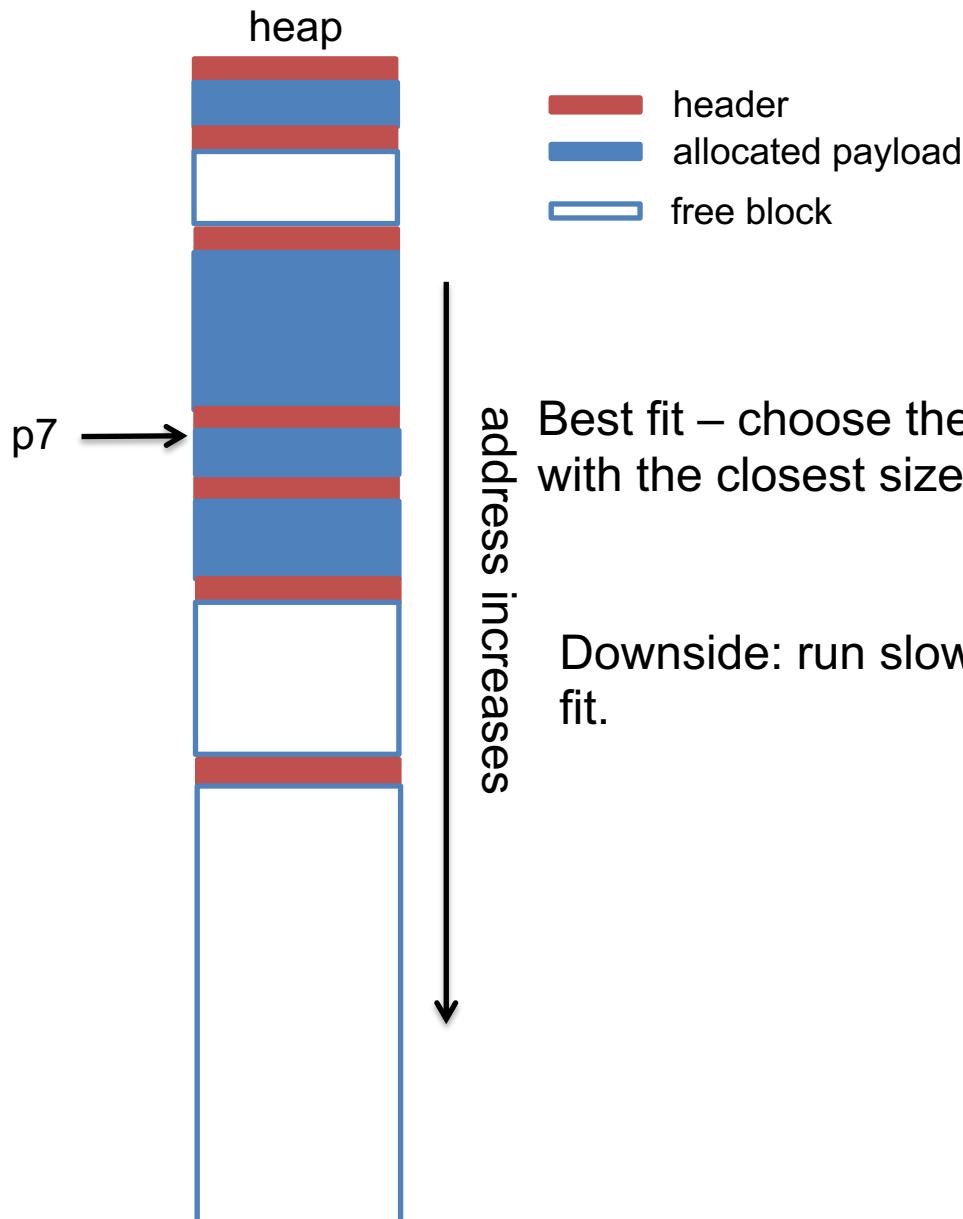
# Best fit



Best fit – choose the free block with the closest size that fits

# Best fit

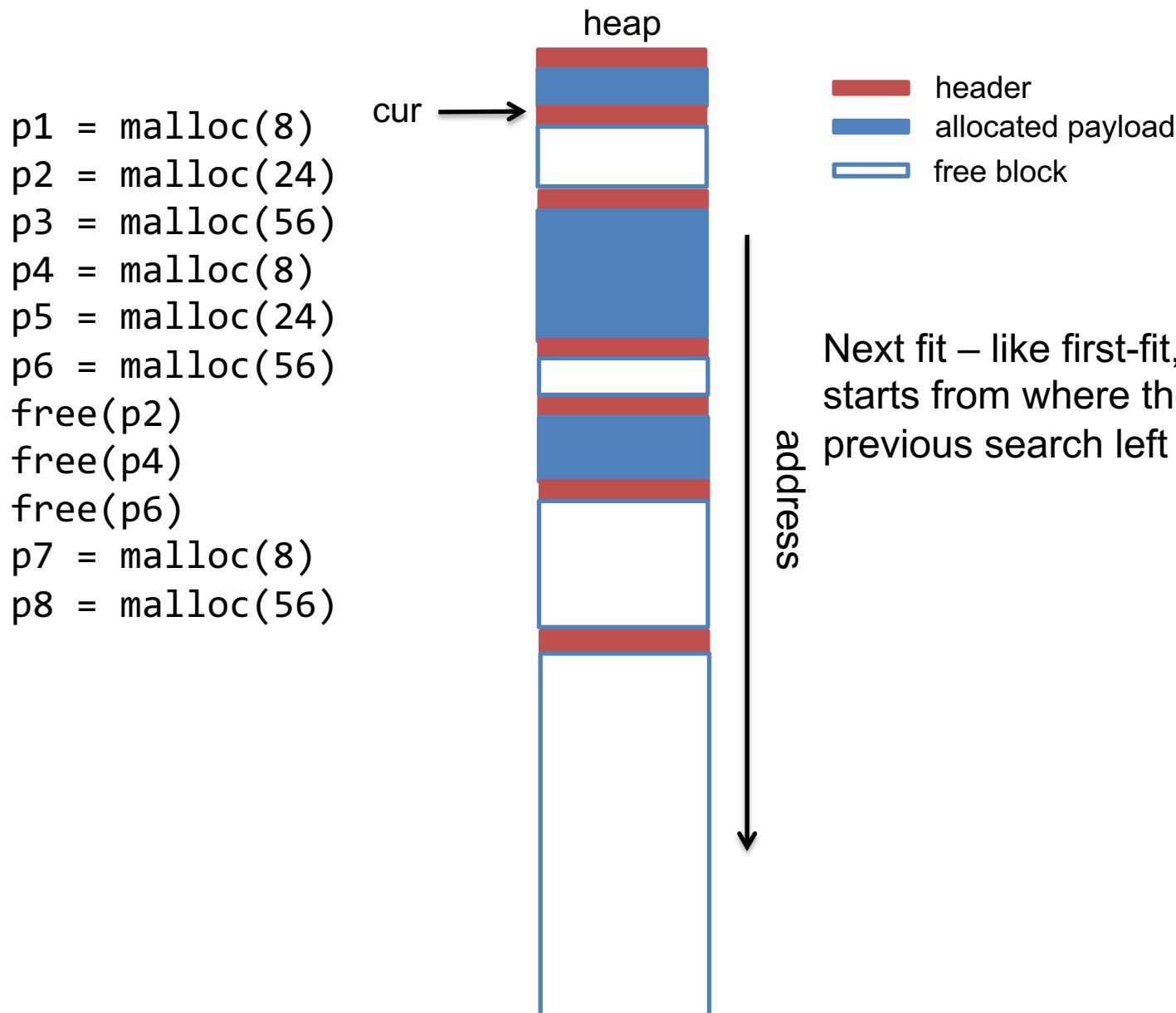
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p4 = malloc(8)
p5 = malloc(24)
p6 = malloc(56)
free(p2)
free(p4)
free(p6)
p7 = malloc(8)
```



Best fit – choose the free block with the closest size that fits

Downside: run slower than first fit.

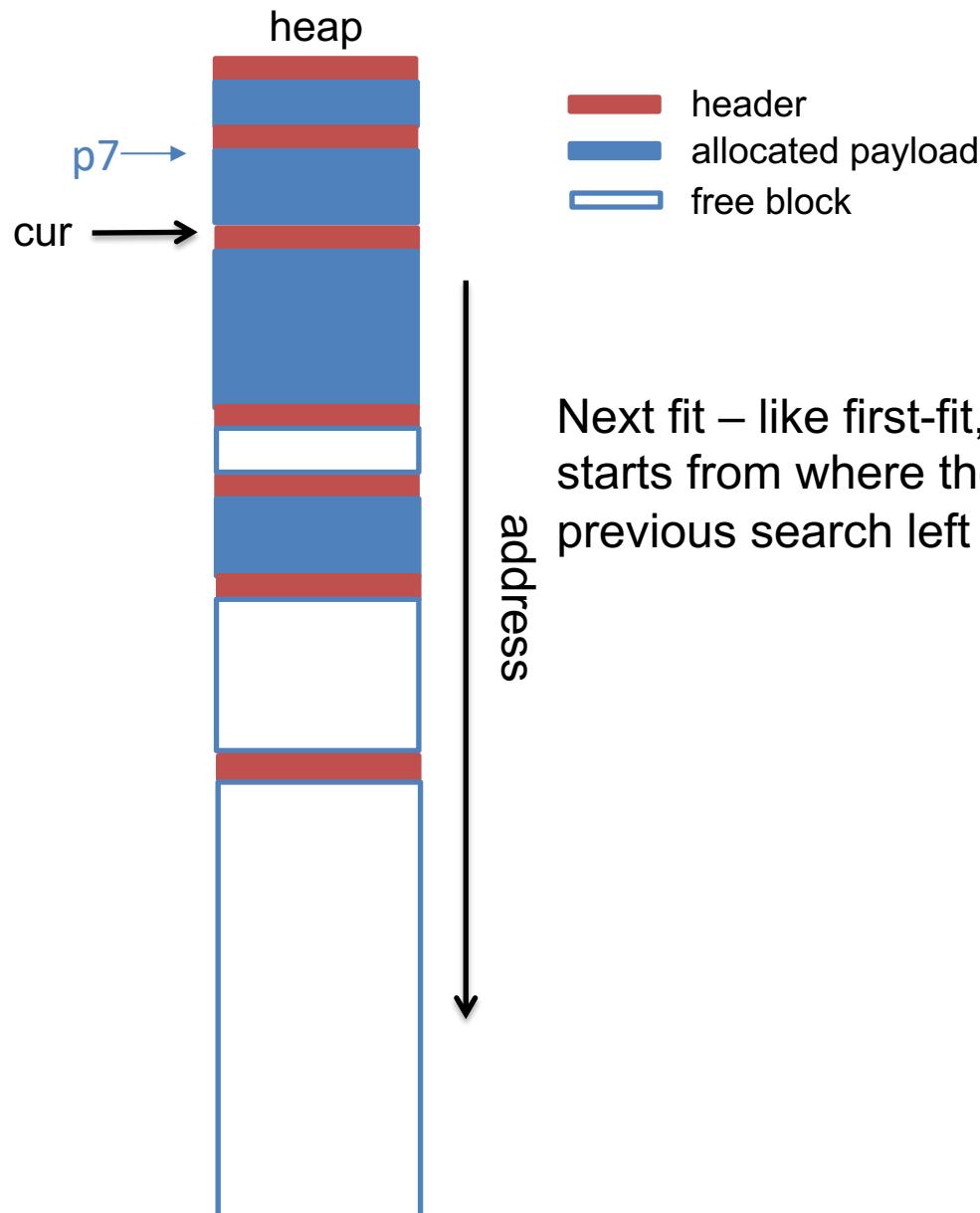
# Next fit



Next fit – like first-fit, but search starts from where the previous search left off.

# Next fit

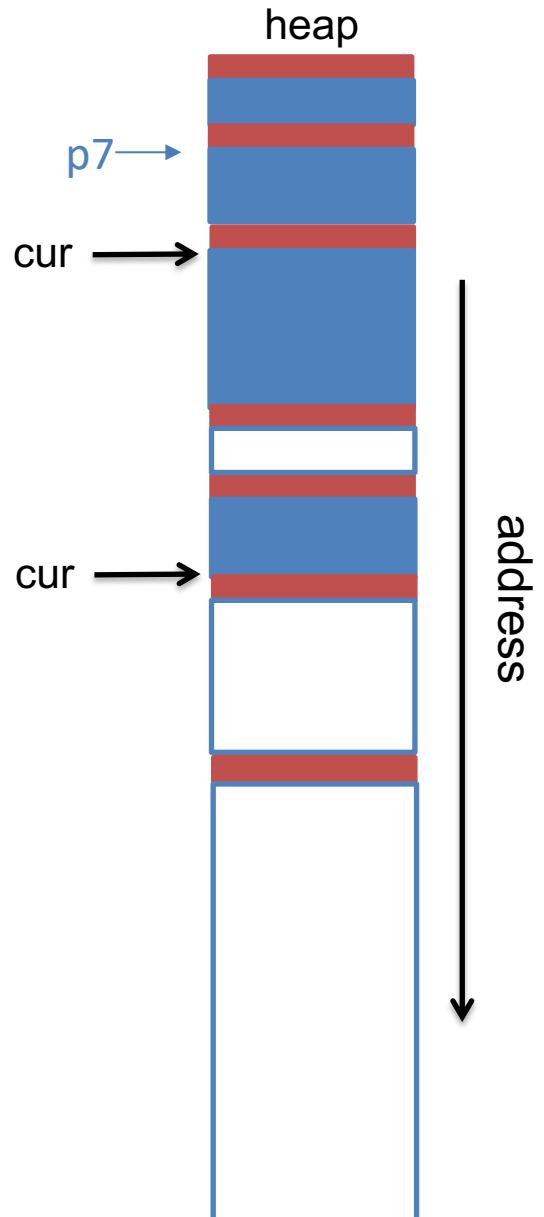
```
p1 = malloc(8)
p2 = malloc(24)
p3 = malloc(56)
p4 = malloc(8)
p5 = malloc(24)
p6 = malloc(56)
free(p2)
free(p4)
free(p6)
p7 = malloc(8)
p8 = malloc(56)
```



Next fit – like first-fit, but search starts from where the previous search left off.

# Next fit

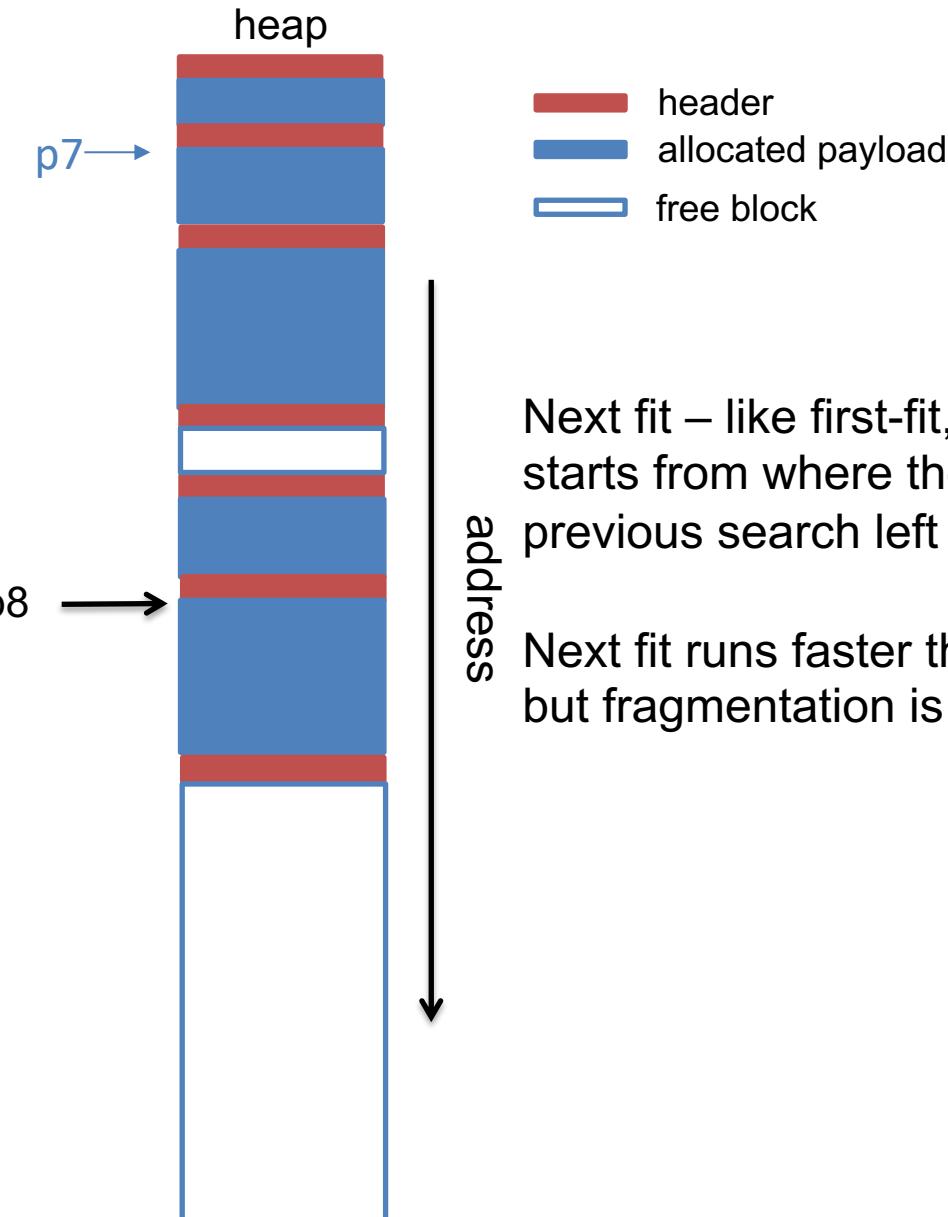
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p7 = malloc(8)
p8 = malloc(56)
```



Next fit – like first-fit, but search starts from where the previous search left off.

# Next fit

```
p1 = malloc(8)
p2 = malloc(24)
p3 = malloc(56)
p4 = malloc(8)
p5 = malloc(24)
p6 = malloc(56)
free(p2)
free(p4)
free(p6)
p7 = malloc(8)
p8 = malloc(56)
```



Next fit – like first-fit, but search starts from where the previous search left off.

Next fit runs faster than first fit, but fragmentation is worse.

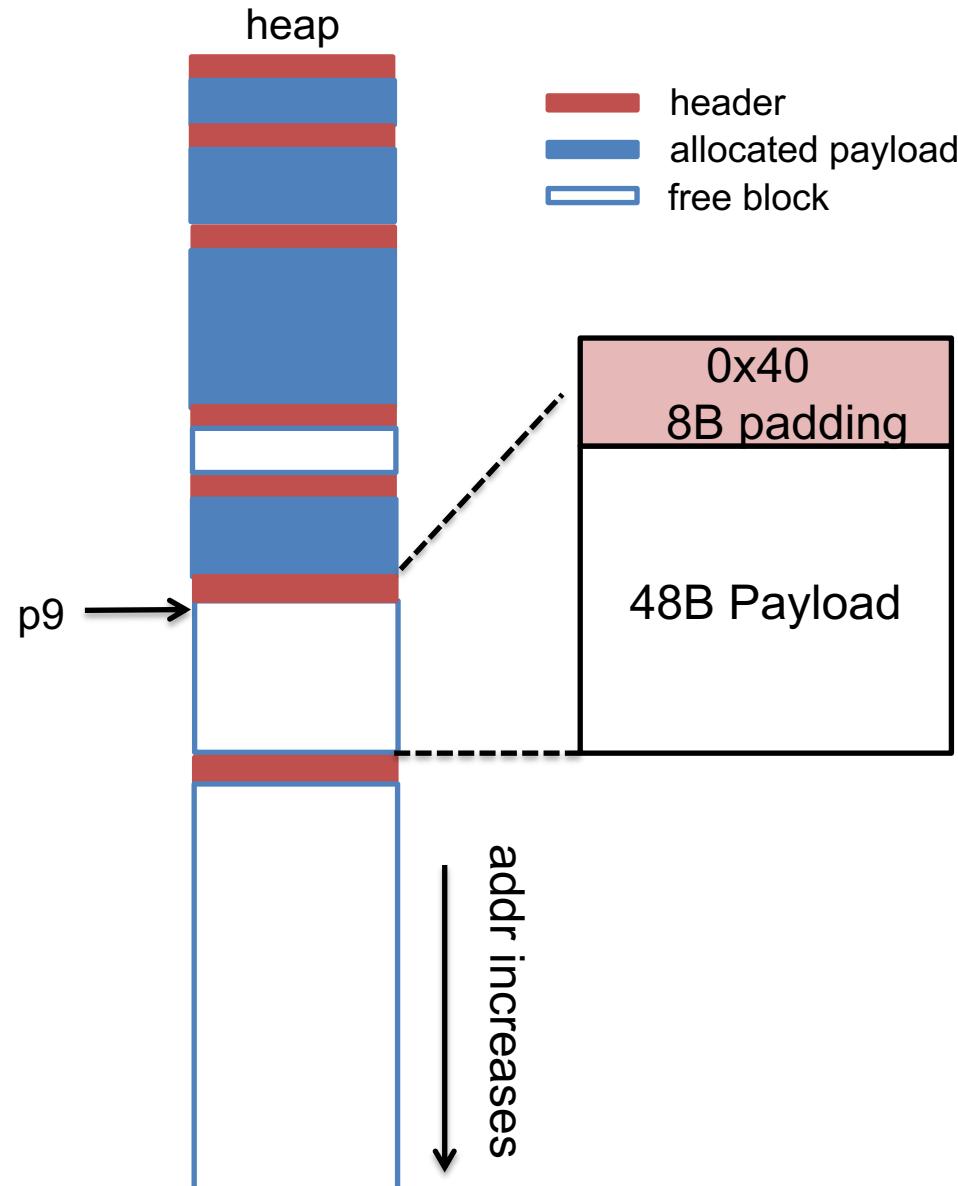
# malloc() in an implicit list

```
void* malloc(unsigned long size) {  
    unsigned long chunk_sz = align(size) + sizeof(header);  
    header *h = find_fit(chunk_sz);  
    //split if chunk is larger than necessary  
    split(h, chunk_sz);  
    set_status(h, true);  
    return header2payload(h);  
}
```

# Splitting a free block

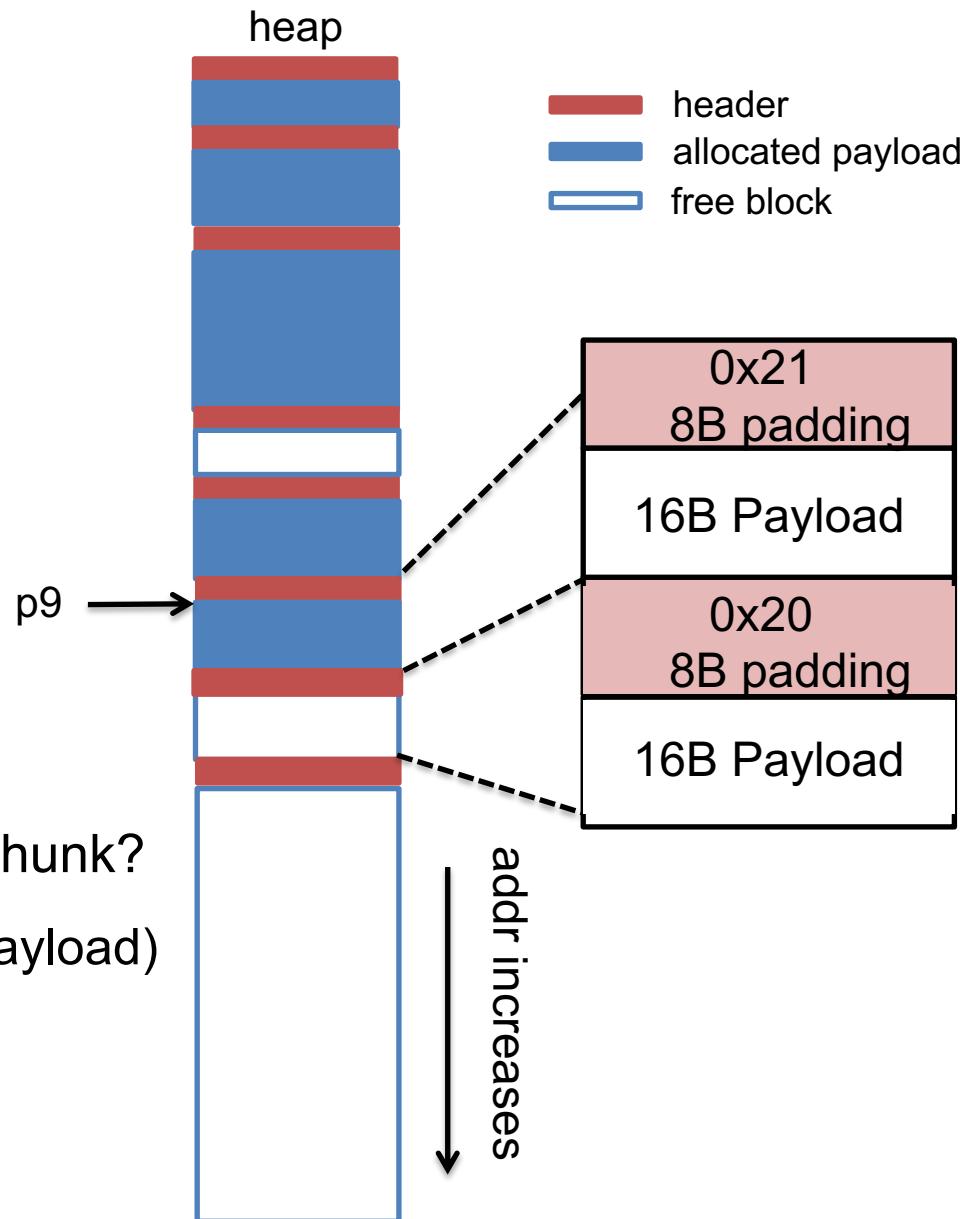
...

p9 = malloc(16)



# Splitting a free block

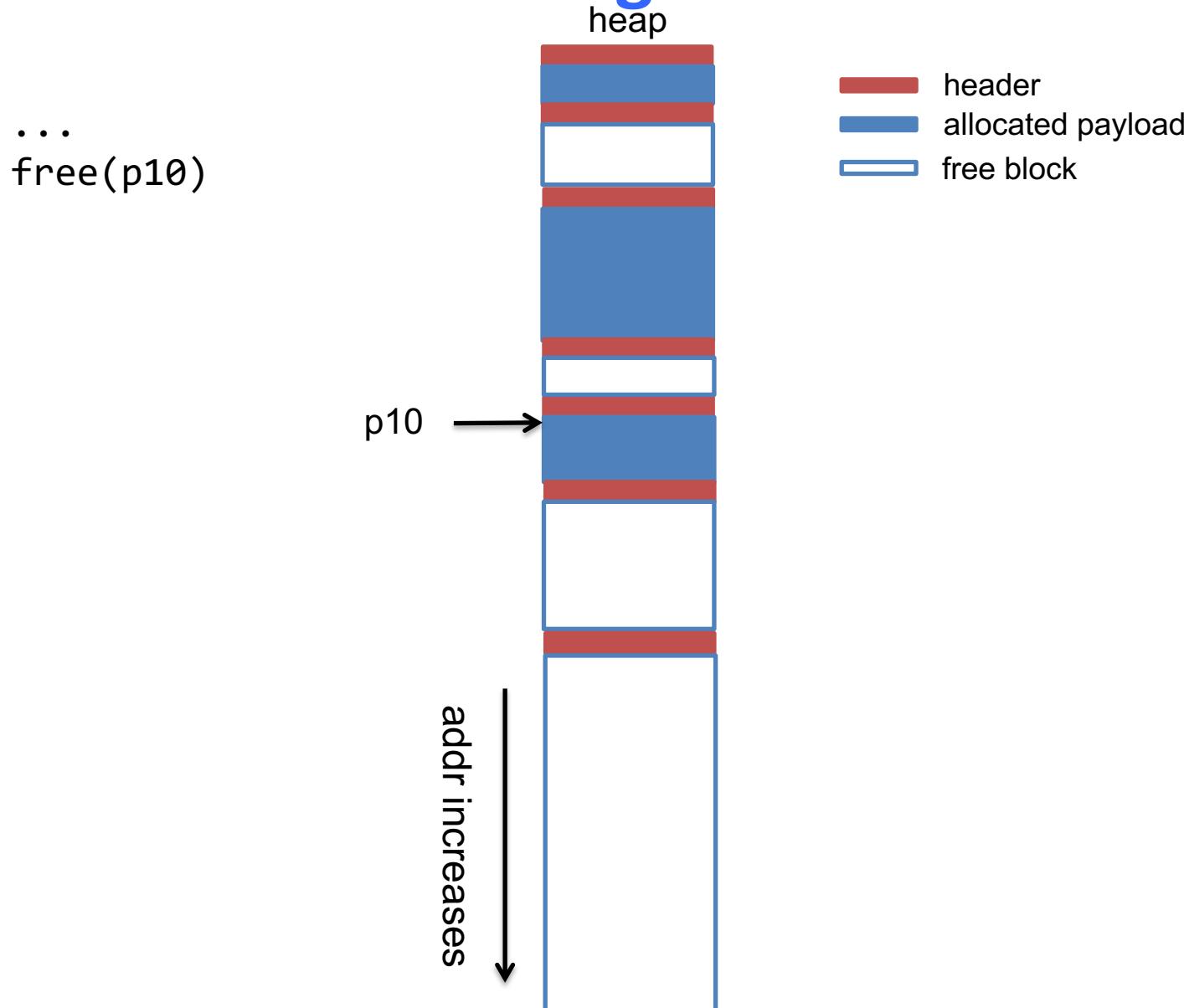
...  
p9 = malloc(16)



Q: what's the smallest chunk?

A: 16 (header)+16(min payload)  
= 32B

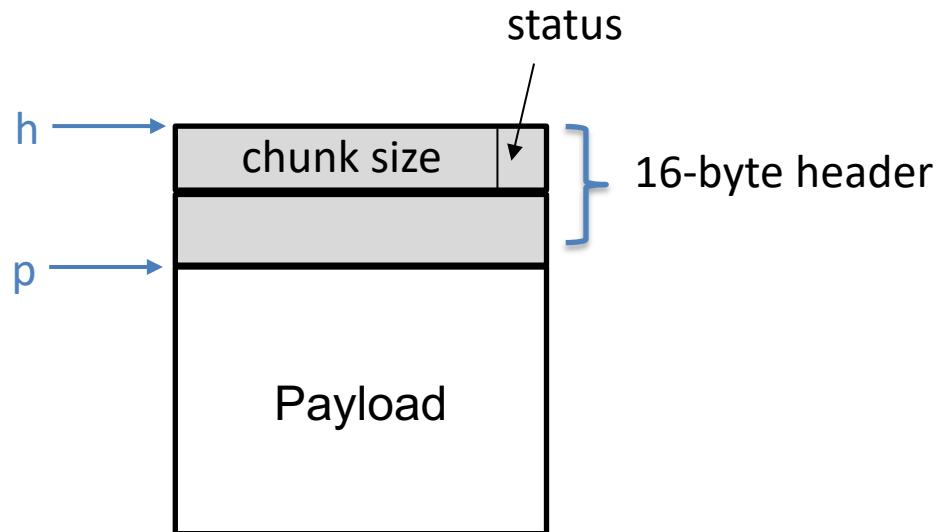
# Coalescing a free block with its next free neighbor



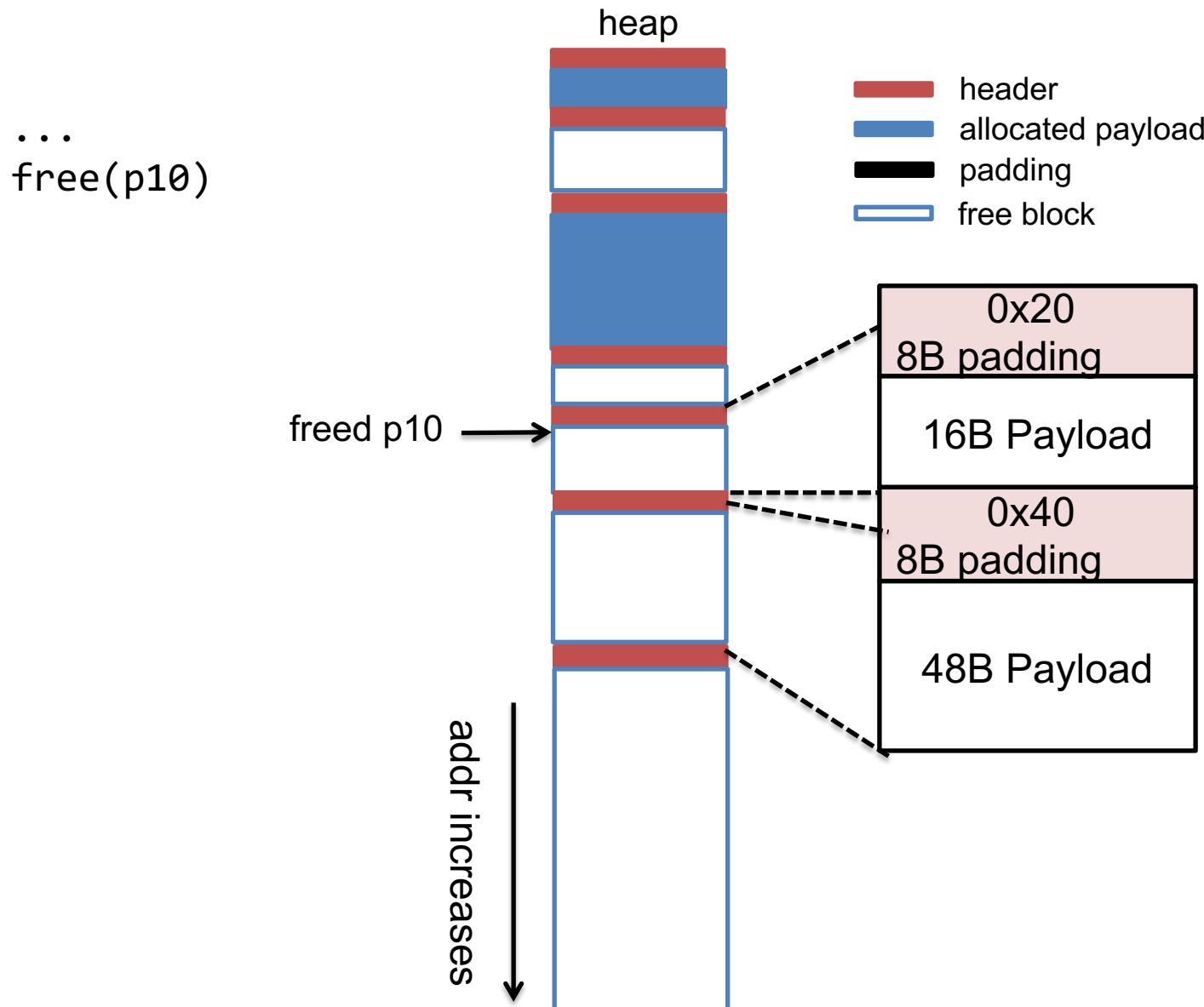
# free() in an implicit list

```
void free(void *p) {  
    header *h = payload2header(p);  
    set_status(h, false);  
    coalesce(h);  
}
```

```
header *payload2header(void *p)  
{  
}  
}
```

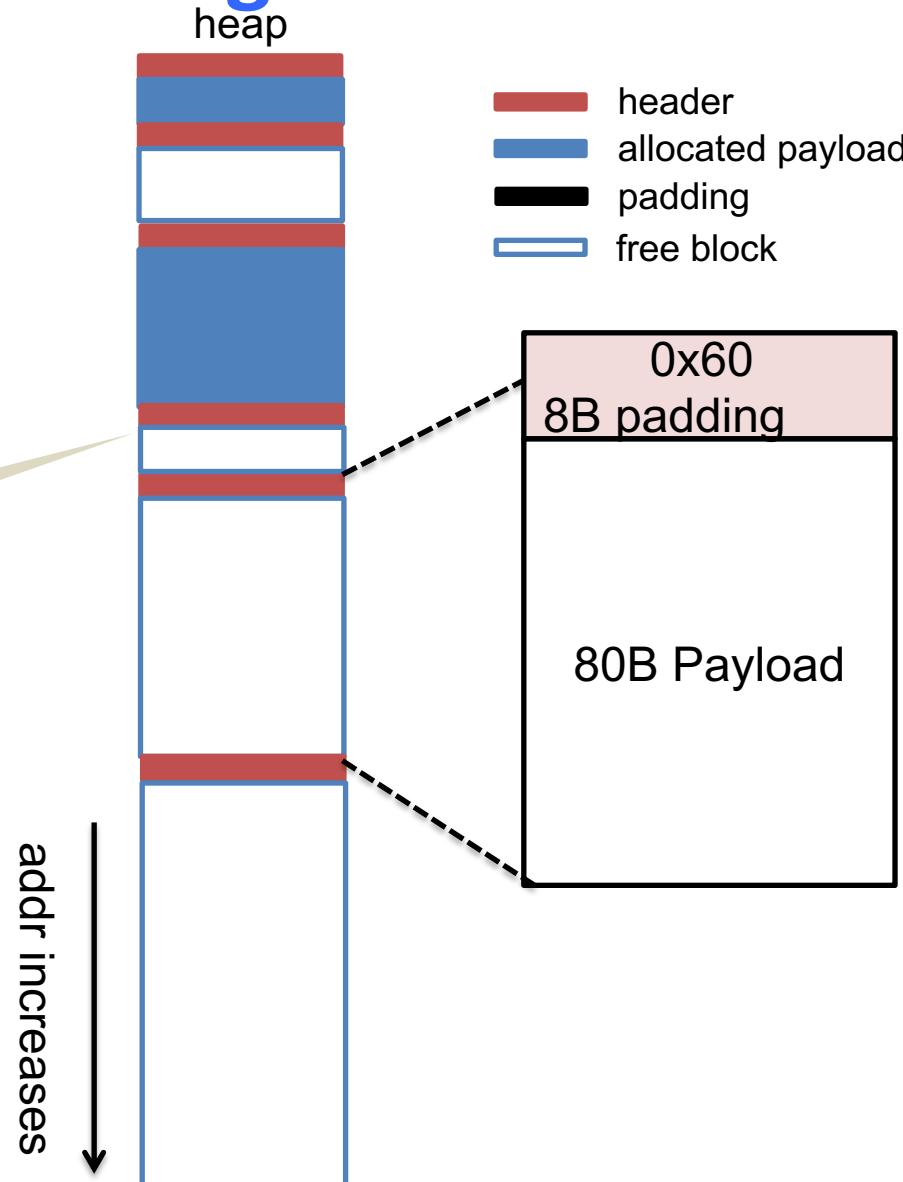


# Coalescing a free block with next free neighbor



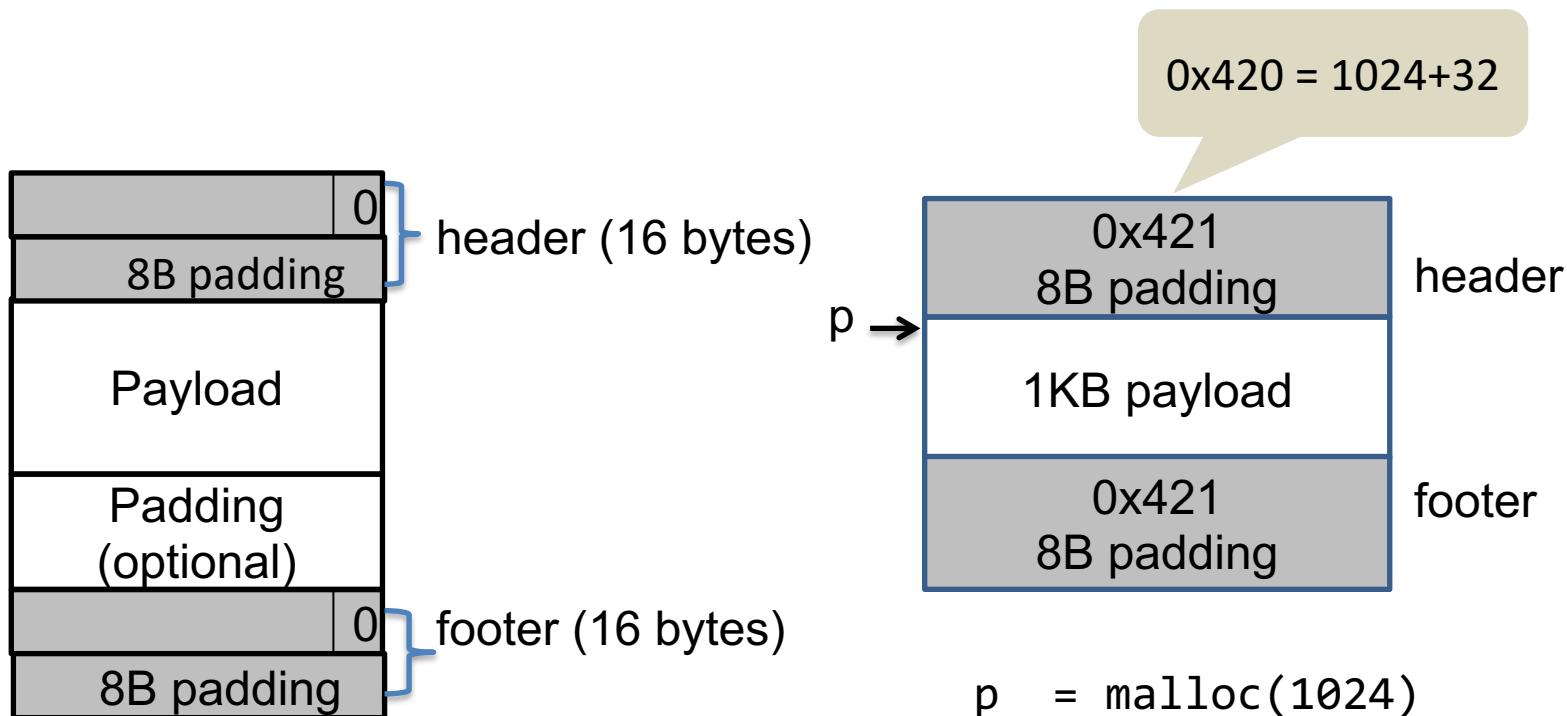
# Coalescing a free block with its next free neighbor

...  
free(p10)

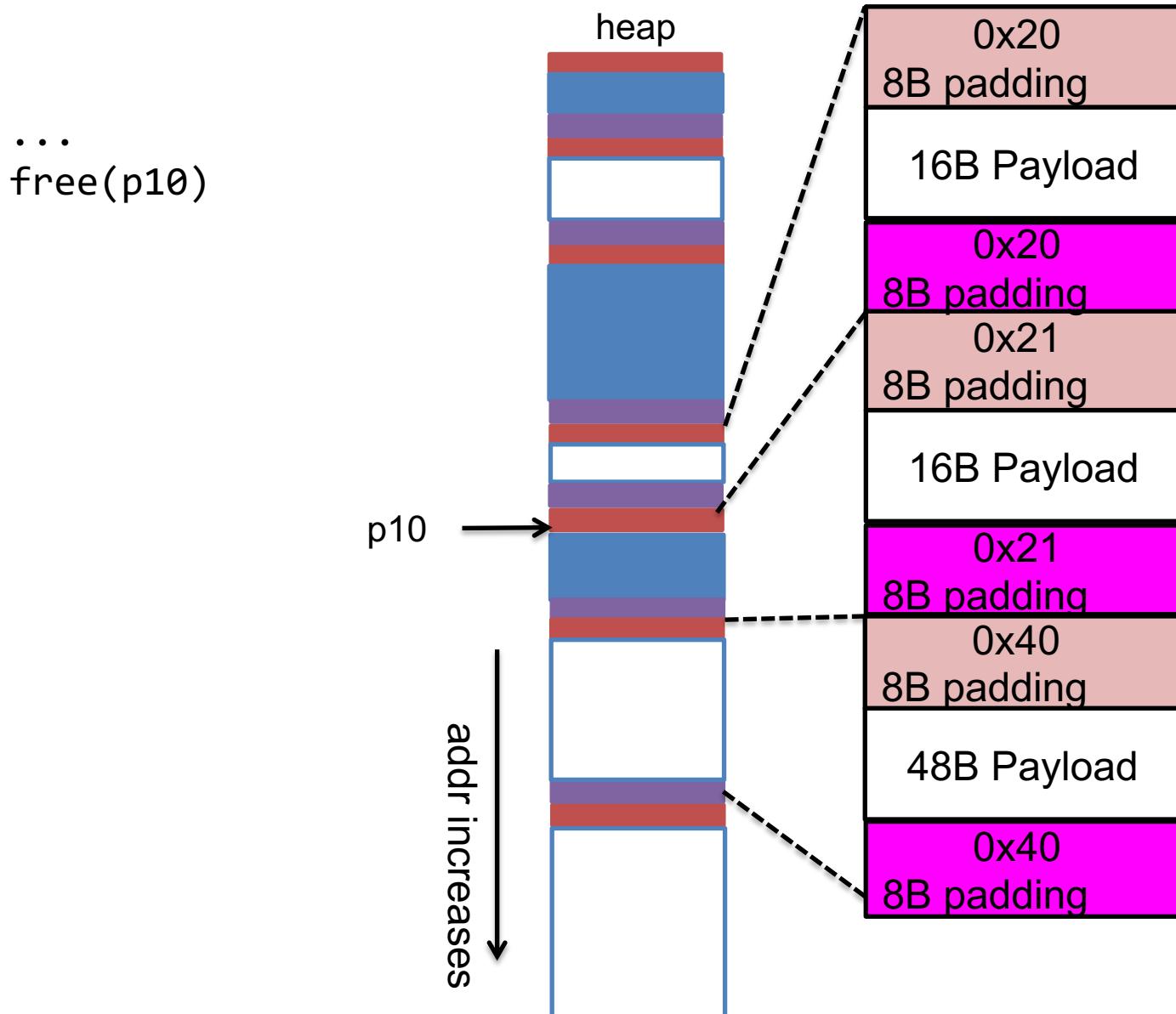


# Use footer to coalesce with previous block

- Duplicate header information into the footer

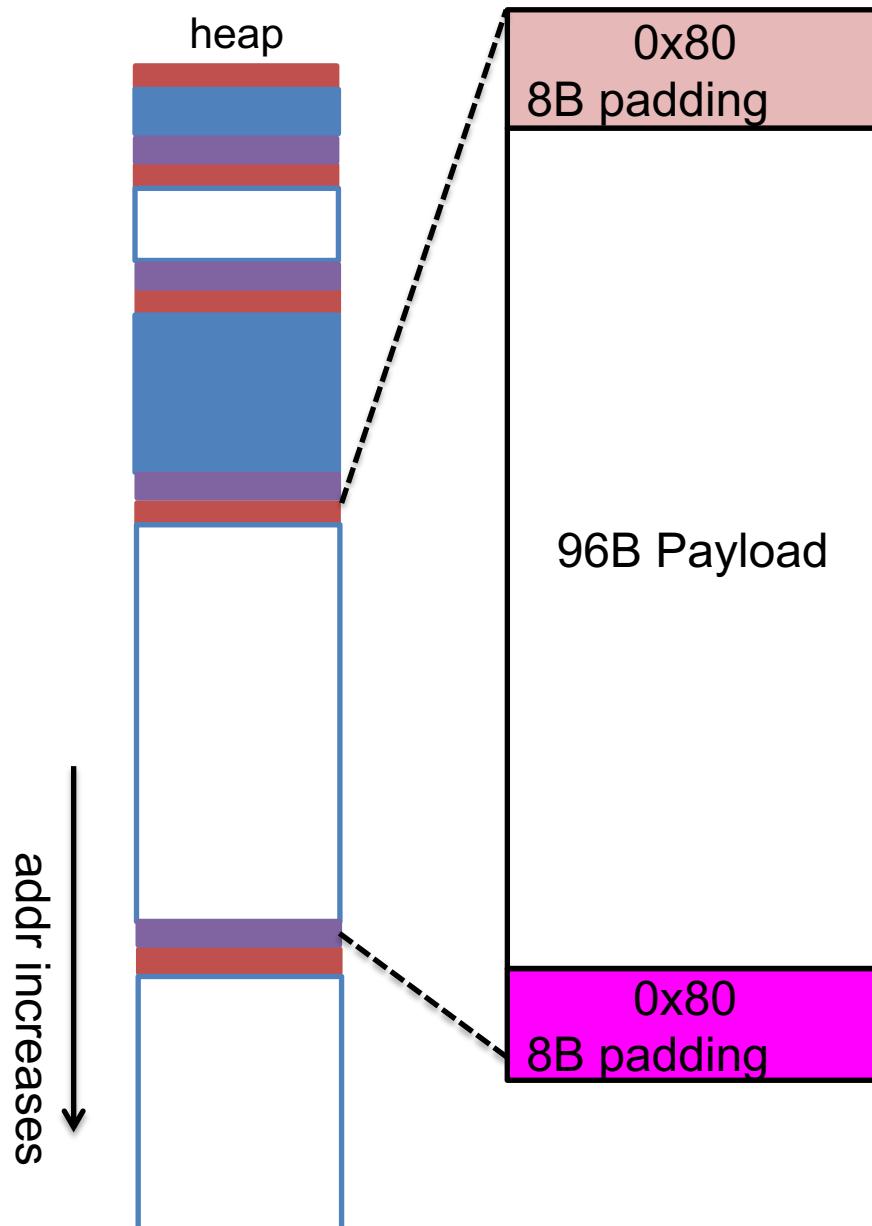


# Coalescing prev and next blocks

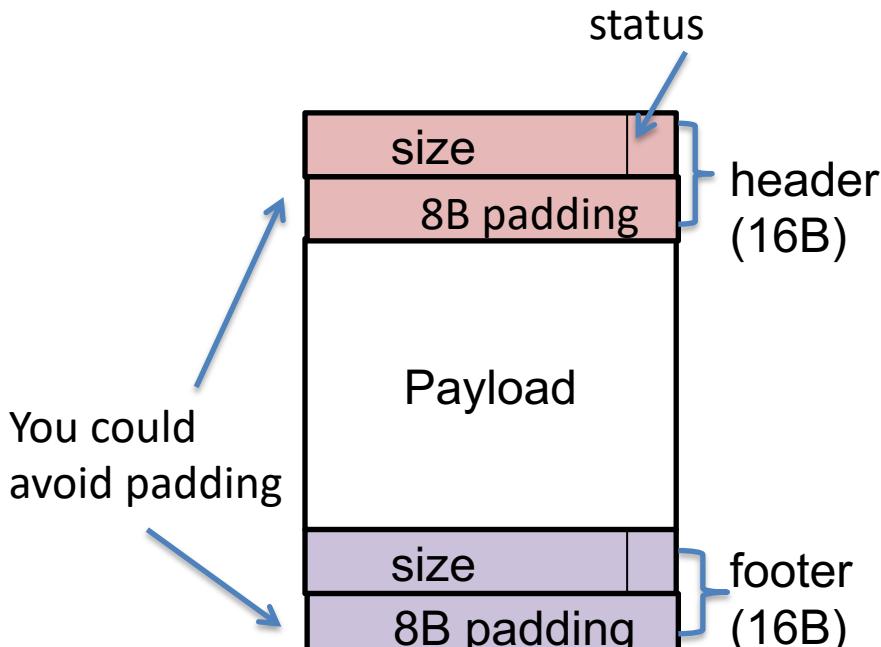


# Coalescing prev and next blocks

...  
free(p10)



# Summary: malloc using implicit list



- We can traverse the entire list of chunks on heap by incrementing pointer with chunk sizes,
  - To allocate, find a block that fits, split if necessary
  - To de-allocate, merge with predecessor and/or successor free blocks
- 
- Question: what's the minimal size of a chunk?  
Answer:  $\geq 16 \text{ (header)} + 16 \text{ (footer)} + 16 \text{ (min payload)} = 48 \text{ bytes}$

# Today's lesson plan

- Explicit list
- Segregated list
- Buddy system

# Explicit free lists

Problems of implicit list:

- Allocation time is linear in # of total (free and allocated) chunks

Explicit free list:

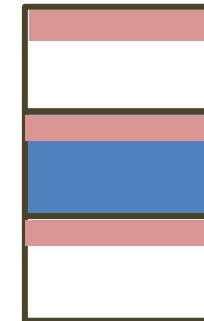
- Maintain a linked list of free chunks only.

# Review: implicit → explicit

Implicit list (header-only)



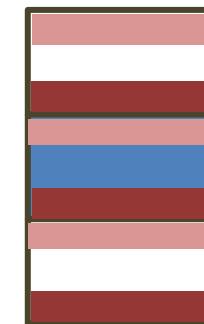
Problem: cannot coalesce with previous free block  
→ contiguous free blocks



Implicit list (header+footer)

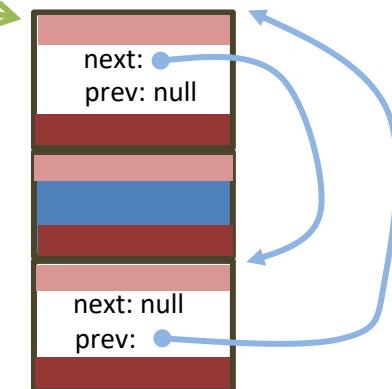


Problem: search for free block scans over allocated blocks



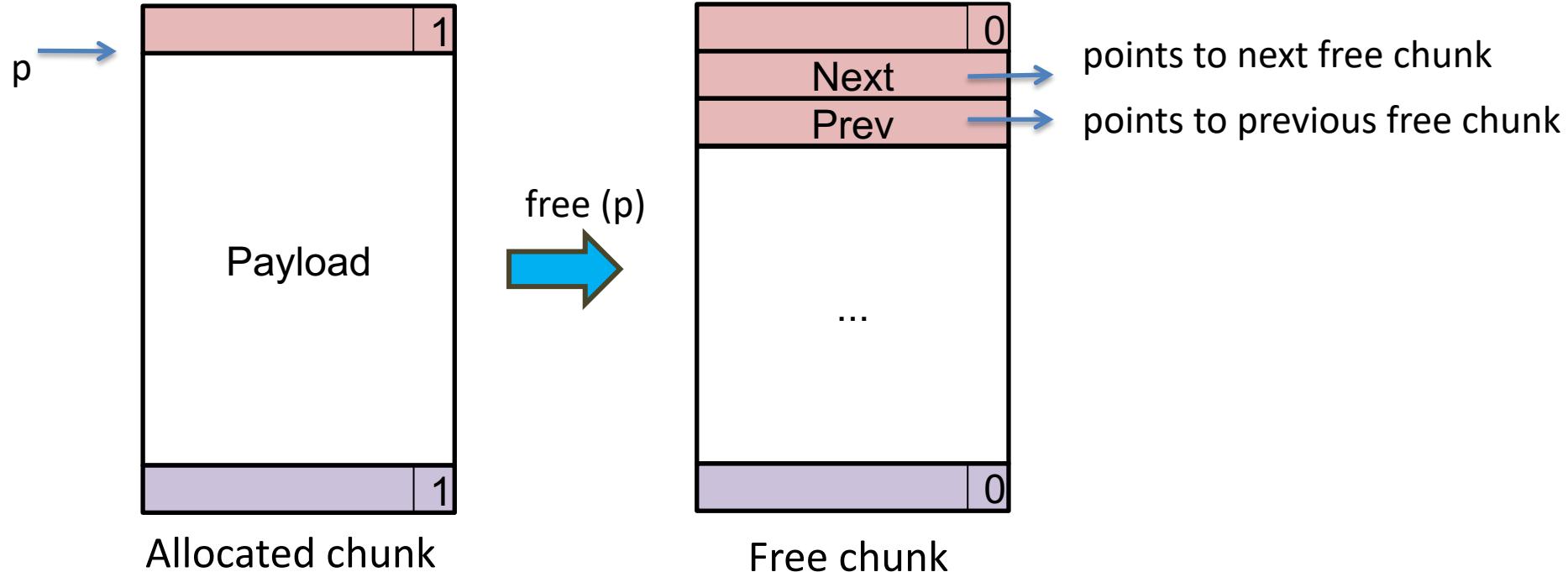
explicit list (header+footer)

head of freelist:



Q: Why use a doubly linked list?

# Explicit free list



- Question: do we need next/prev fields for allocated blocks?

Answer: No. We do not need to chain together allocated blocks. We can still traverse all blocks (free and allocated) as in the case of implicit list.

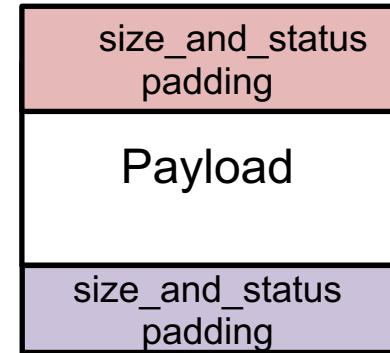
- Question: what's the minimal size of a chunk?

Answer: 16 (header) + 16 (footer) + 8 (next pointer) + 8 (previous pointer) = 48 bytes

# Explicit list: implementation

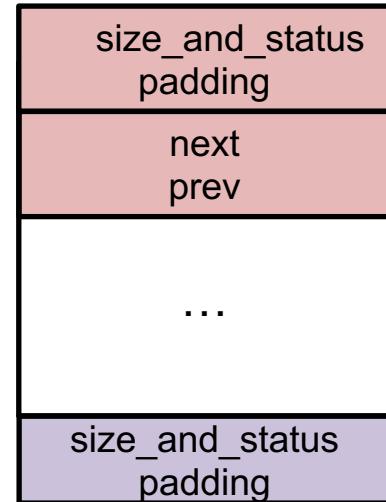
```
typedef struct {  
    unsigned long size_and_status;  
    unsigned long padding;  
} header;
```

Allocated chunk:



```
typedef struct free_hdr {  
    header common_header;  
    struct free_hdr *next;  
    struct free_hdr *prev;  
} free_hdr;
```

Free chunk:

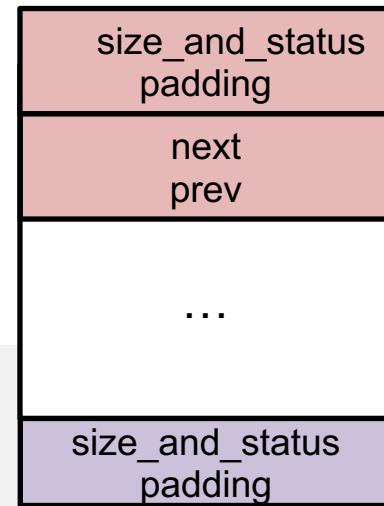


# Explicit list: initialization

```
typedef struct free_hdr {  
    header common_header;  
    struct free_hdr *next;  
    struct free_hdr *prev;  
} free_hdr;  
  
free_hdr *freelist = NULL;
```

```
//initialize a region of memory of size 'sz'  
//with start address 'h' as a free chunk  
void init_free_chunk(free_hdr *h, size_t sz)  
{  
  
    set_size_status(&h->common_header, sz, false);  
    h->prev = h->next = NULL;  
    set_size_status(get_footer_from_header(&h->common_header), sz, false);  
}
```

```
void init() {  
    free_hdr *h = get_block_from_OS(INIT_ALLOC_SZ);  
    init_free_chunk(h, sz);  
    insert(&freelist, h);  
}
```



# Explicit list: allocate

```
void *malloc(size_t s) {
    size_t csz = align(s) + 2*sizeof(header); //min chunk size required
    free_hdr *h = first_fit(csz);
    //if h=NULL (not enough space), ask OS to enlarge heap
    free_hdr *newchunk = split(h, csz);
    if (newchunk)
        insert(&freelist, newchunk);
    set_status(h, true);
    return header2payload(h);
}
free_hdr *first_fit(size_t sz) {
}
```

# Explicit list: allocate

```
void *malloc(size_t s) {
    size_t csz = align(s) + 2*sizeof(header); //min chunk size required
    free_hdr *h = first_fit(csz);
    //if h=NULL (not enough space), ask OS to enlarge heap
    free_hdr *newchunk = split(h, csz);
    if (newchunk)
        insert(&freelist, newchunk);
    set_status(h, true);
    return header2payload(h);
}
free_hdr *first_fit(size_t sz) {
    free_hdr *h = freelist;
    while (h) {
        if (get_size(&h->common_header)>= sz) {
            delete(&freelist, h);
            break;
        }
        h = h->next;
    }
    return h;
}
```

# Explicit list: allocate

```
void *malloc(size_t s) {
    size_t csz = align(s) + 2*sizeof(header); //min chunk size required
    free_hdr *h = first_fit(csz);
    //if h=NULL (not enough space), ask OS to enlarge heap
    free_hdr *newchunk = split(h, csz);
    if (newchunk)
        insert(&freelist, newchunk);
    set_status(h, true);
    return header2payload(h);
}

free_hdr *split(free_hdr *h, size_t csz)
{
}
}
```

# Explicit list: allocate

```
void *malloc(size_t s) {
    size_t csz = align(s) + 2*sizeof(header); //min chunk size required
    free_hdr *h = first_fit(csz);
    //if h=NULL (not enough space), ask OS to enlarge heap
    free_hdr *newchunk = split(h, csz);
    if (newchunk)
        insert(&freelist, newchunk);
    set_status(h, true);
    return header2payload(h);
}

free_hdr *split(free_hdr *h, size_t csz)
{
    size_t remain_sz = get_size(&h->common_header) - csz;
    if (remain_sz < MIN_CHUNK_SZ)
        return NULL;
    init_free_chunk(h, csz);
    free_hdr *newchunk = next_chunk(h);
    init_free_chunk(newchunk, remain_sz);
    return newchunk;
}
```

# Explicit list: free

```
void free(void *p) {
    header *h = payload2header(p);
    init_free_chunk((free_hdr *)h, get_size(h));

    header *next = next_chunk(h);
    if (!get_status(next)) {
        delete(&freelist, next);
        h = coalesce((free_hdr *)h, (free_hdr *)next);
    }
    header *prev = prev_chunk(h);
    if (!get_status(prev)) {
        delete(&freelist, prev);
        h = coalesce((free_hdr *)prev, (free_hdr *)h);
    }
    insert(&freelist, (free_hdr *)h);
}

free_hdr *coalesce(free_hdr *h, free_hdr *other) {
    //merge h and other into a single free chunk
}
```

# Segregated list

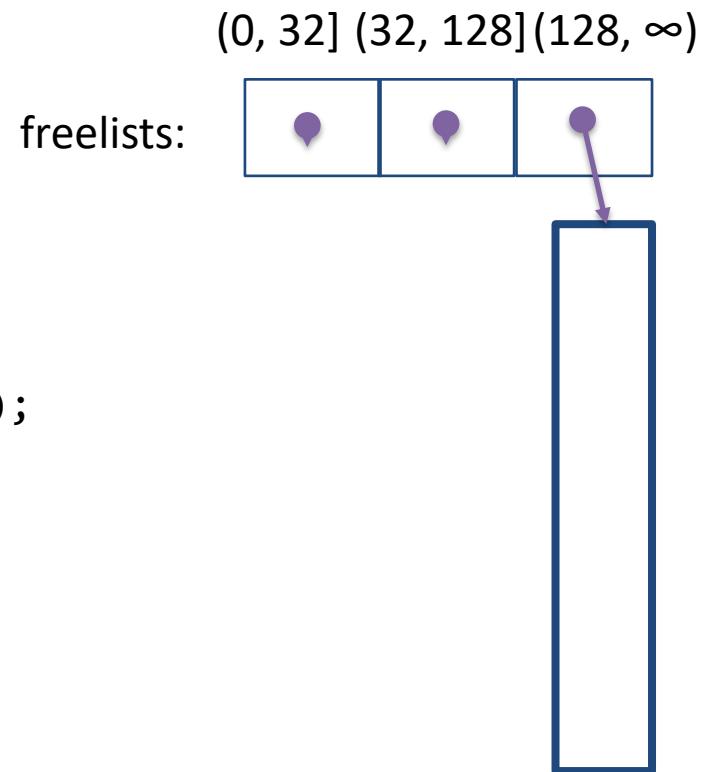
- Idea: keep multiple freelists
  - each freelist contains chunks of similar sizes

# Segregated list: initialize

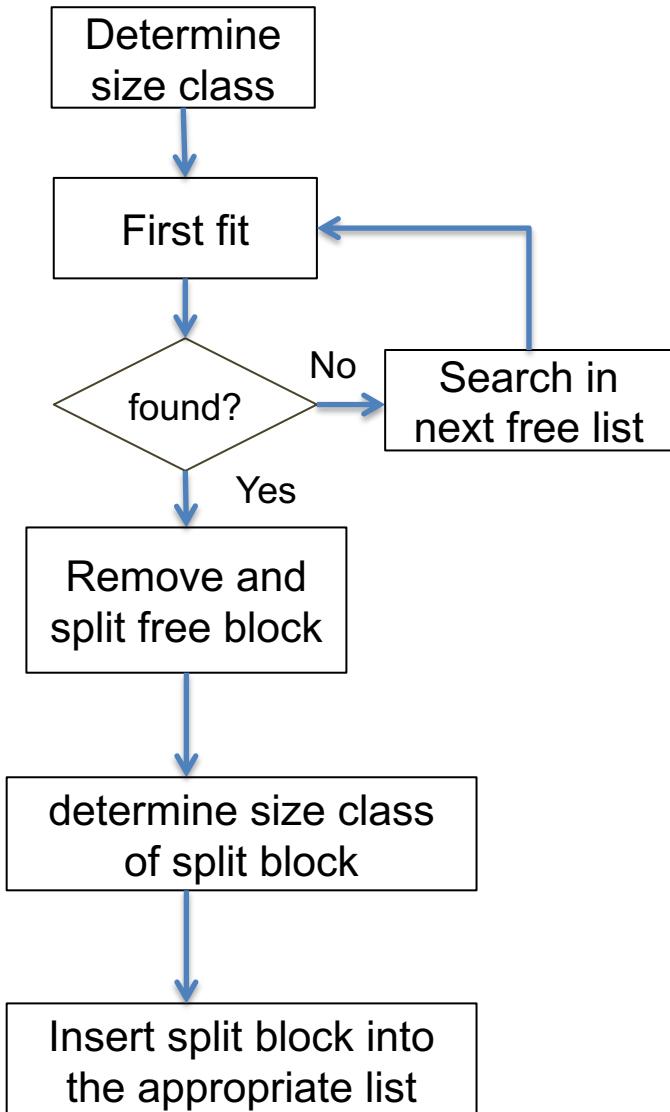
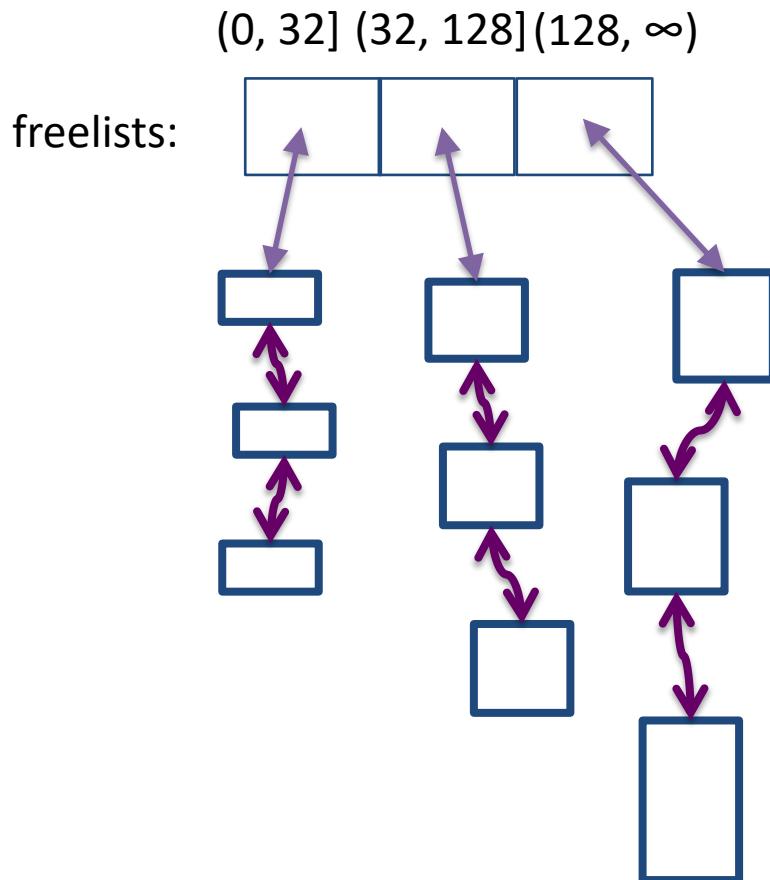
```
#define NLISTS 3
free_hdr* freelists[NLISTS];
size_t size_classes[NLISTS] = {32, 128, (size_t)-1};

int which_freelist(size_t s) {
    int ind = 0;
    while (s > size_classes[ind])
        ind++;
    return ind;
}

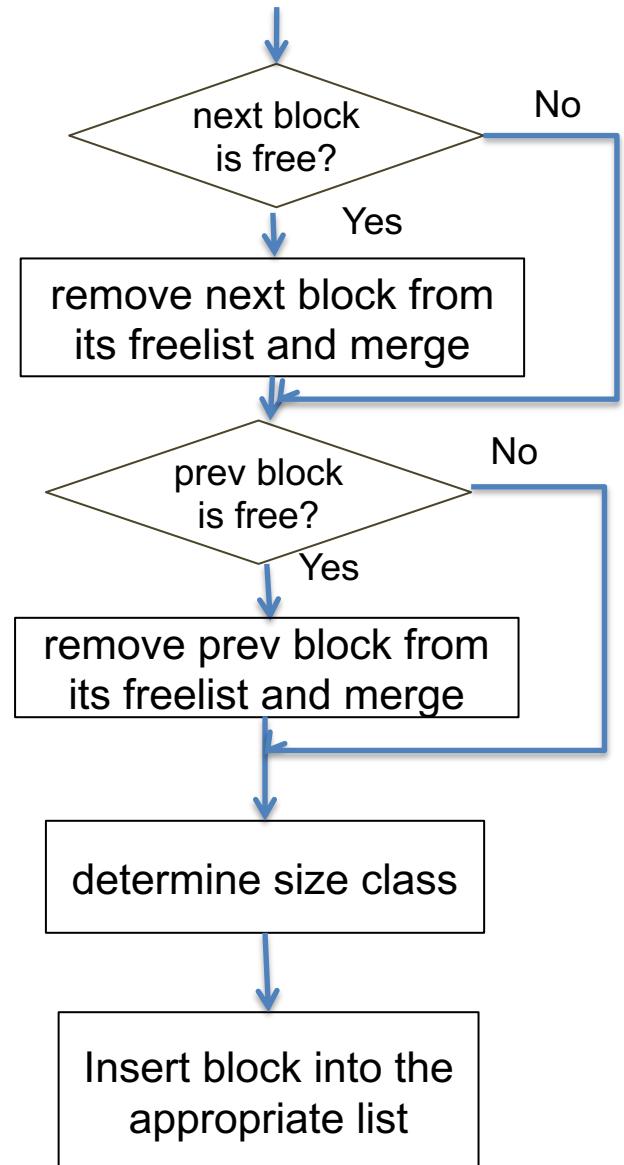
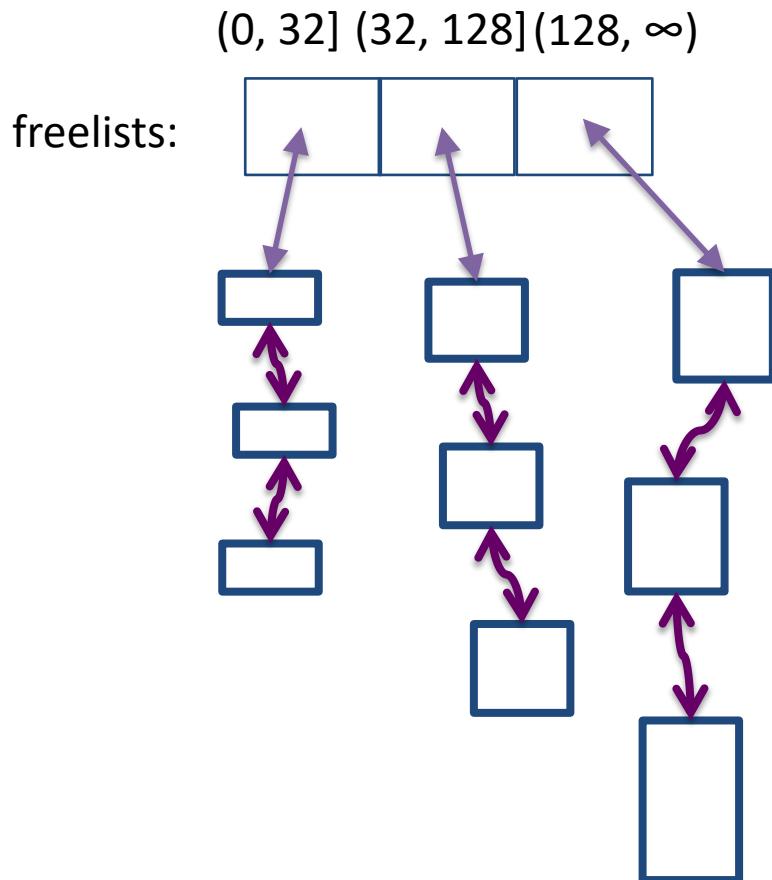
void init() {
    free_hdr *h = get_block_from_OS(1024);
    freelist[which_freelist(1024)] = h;
}
```



# Segregated list: allocation



# Segregated list: free



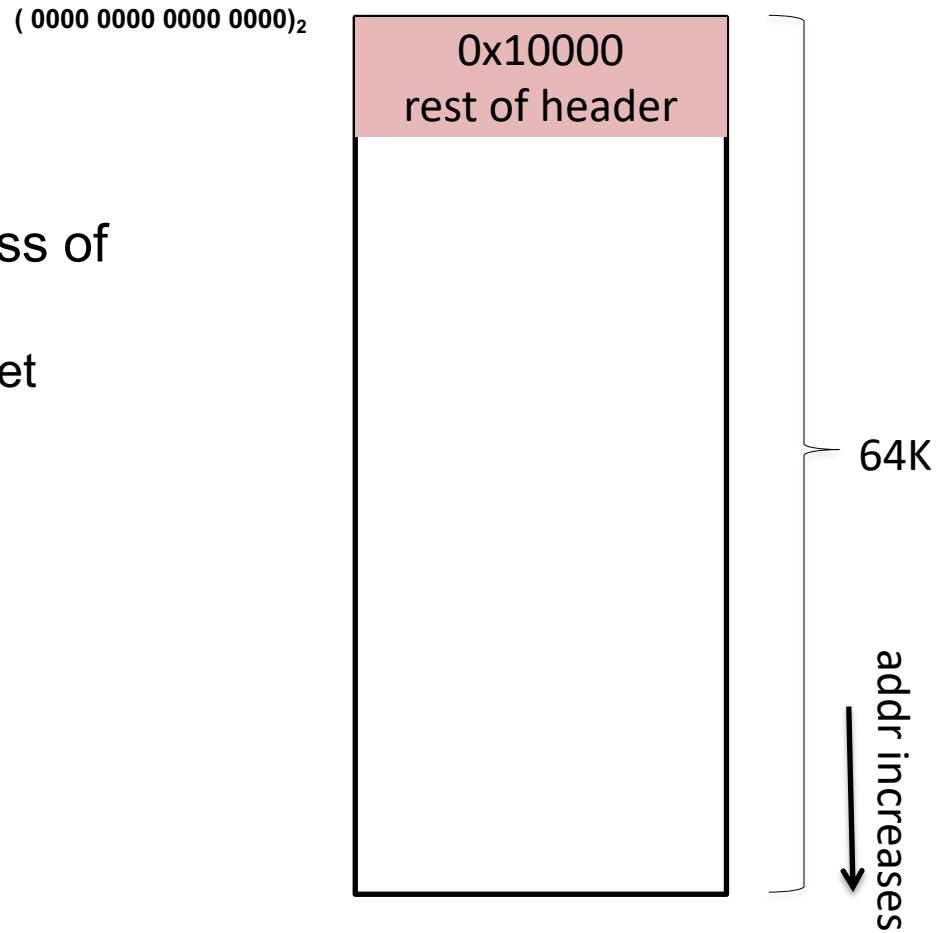
# Buddy System

- A special case of segregated list
  - each freelist has *identically-sized* blocks
  - block sizes are powers of 2
- Advantage over a normal segregated list?
  - Less search time (no need to search within a freelist)
  - Less coalescing time
- Adopted by Linux kernel and jemalloc

# Simple binary buddy system

Initialize:

- assume heap starts at the address of all zeros
  - Implementation can add an offset



# Binary buddy system: allocate

```
p = malloc(15000);
```

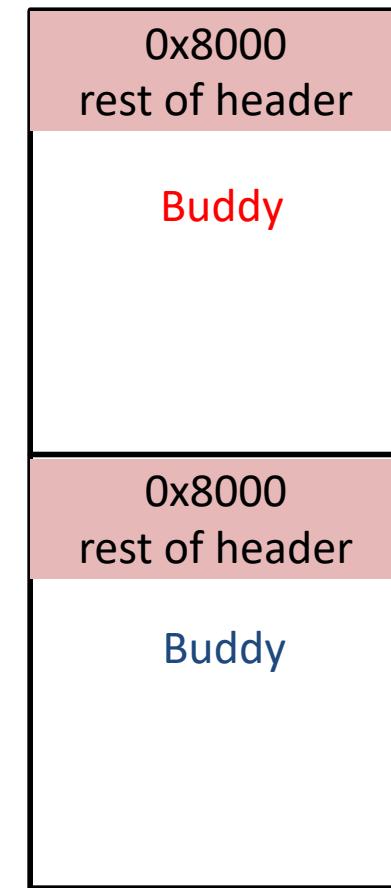
Recursive split in half until having the right size

- insert free buddy into appropriate freelist

Addresses of buddies at size  $2^m$  differ in exactly 1-bit at position m (from right)

( $0000\ 0000\ 0000\ 0000$ )<sub>2</sub>

( $1000\ 0000\ 0000\ 0000$ )<sub>2</sub>



32K

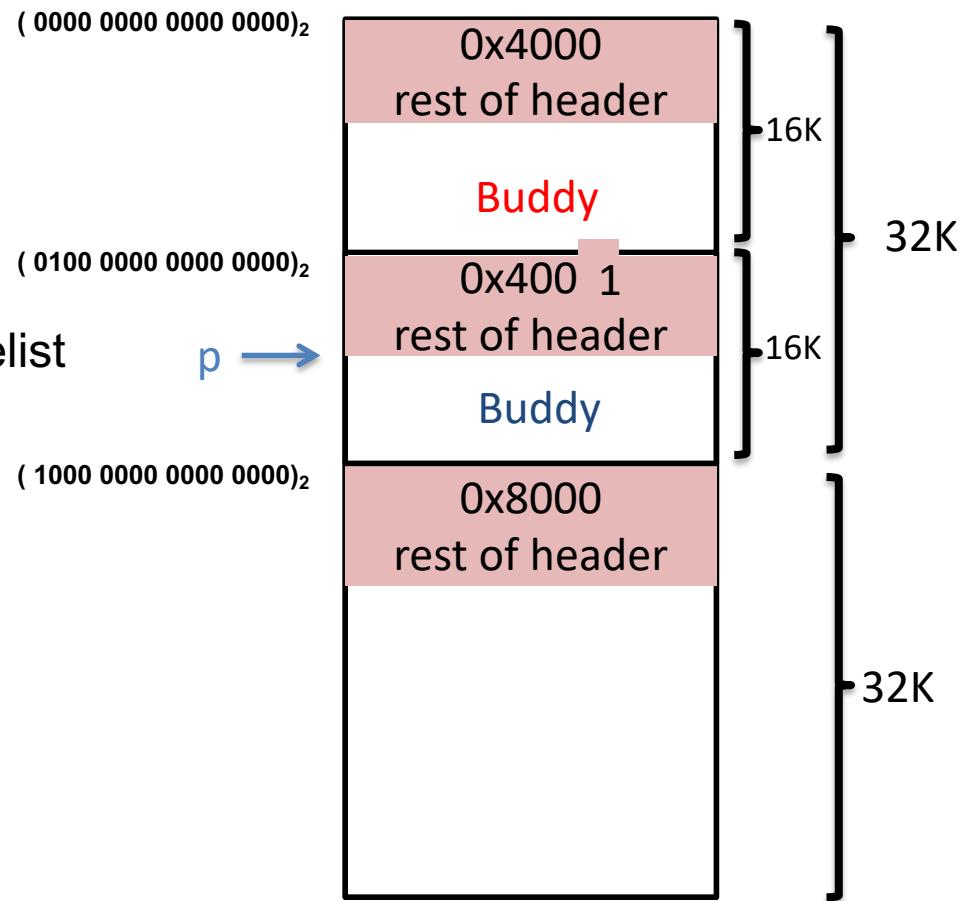
32K

# Binary buddy system: allocate

```
p = malloc(15000);
```

Recursive split in half until having  
the right size

- insert free buddy into appropriate freelist



# Binary buddy system: free

free(p);

Recursively merge block with buddy

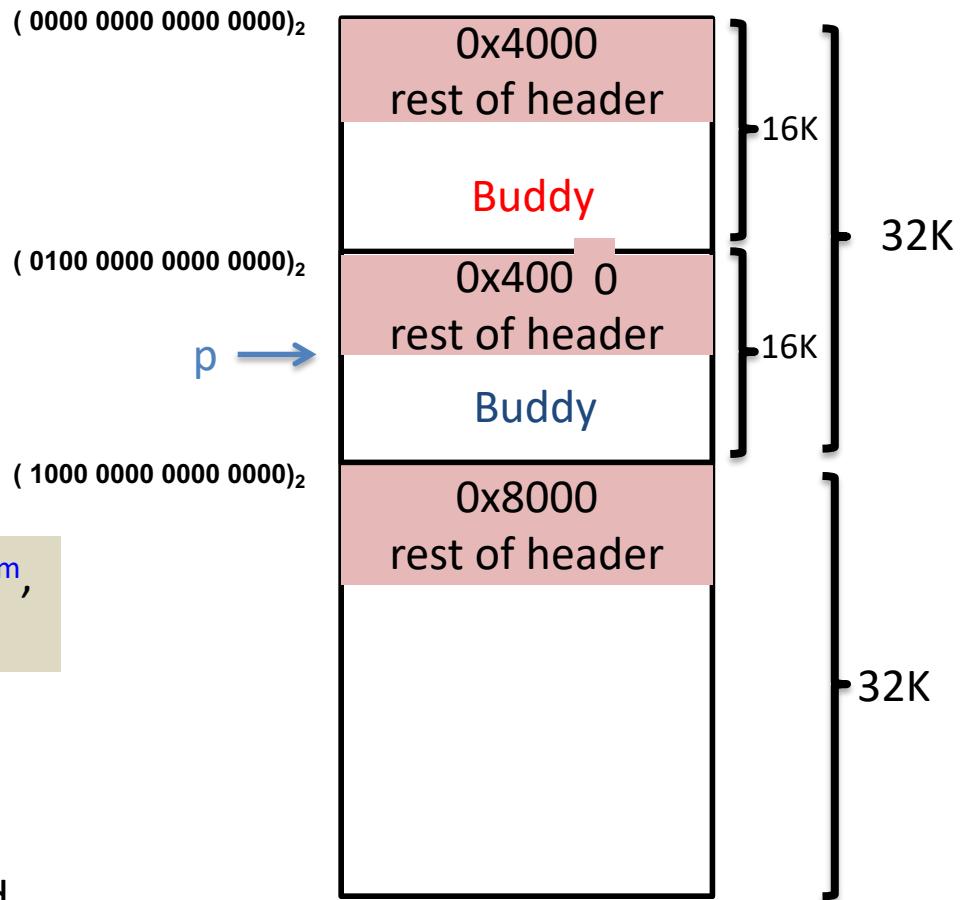
1. Calculate addr of buddy block,  
determine buddy status

Question: given addr  $a$  of block with size  $2^m$ ,  
how to calculate its buddy's address?

$a \wedge (1 << m)$



any bit XOR 0 = unchanged  
any bit XOR 1 = flipped

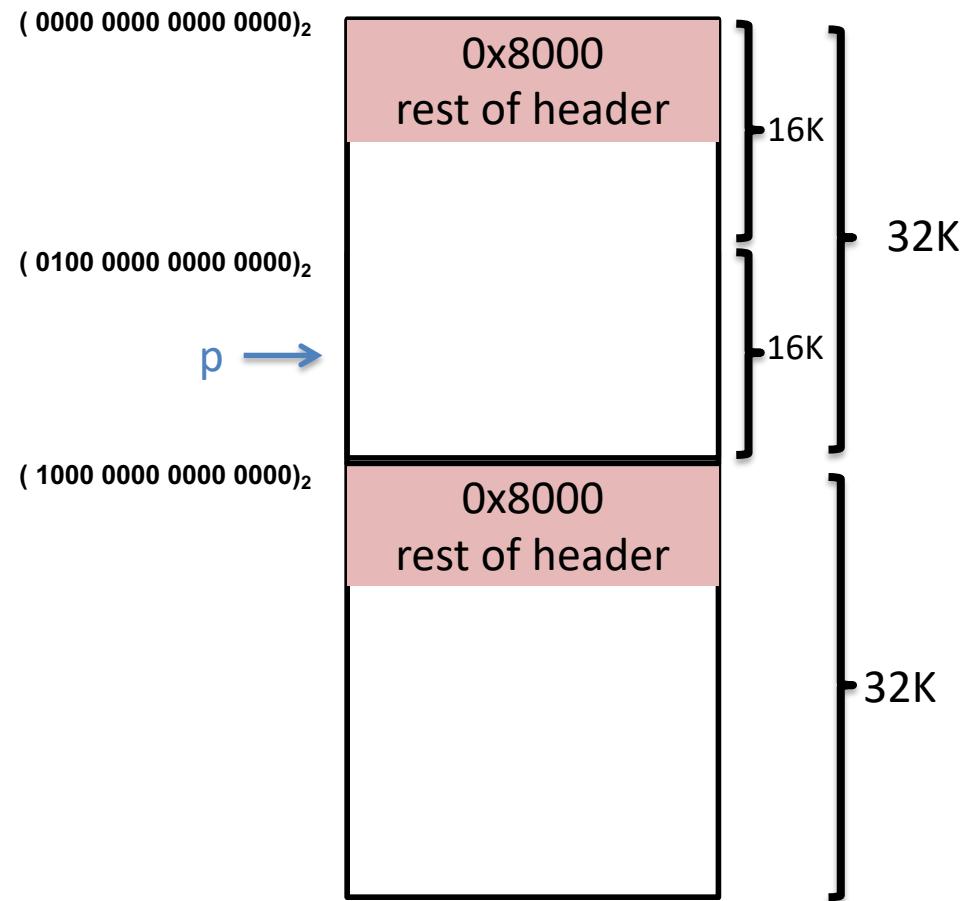


# Binary buddy system: free

free(p);

If buddy is free:

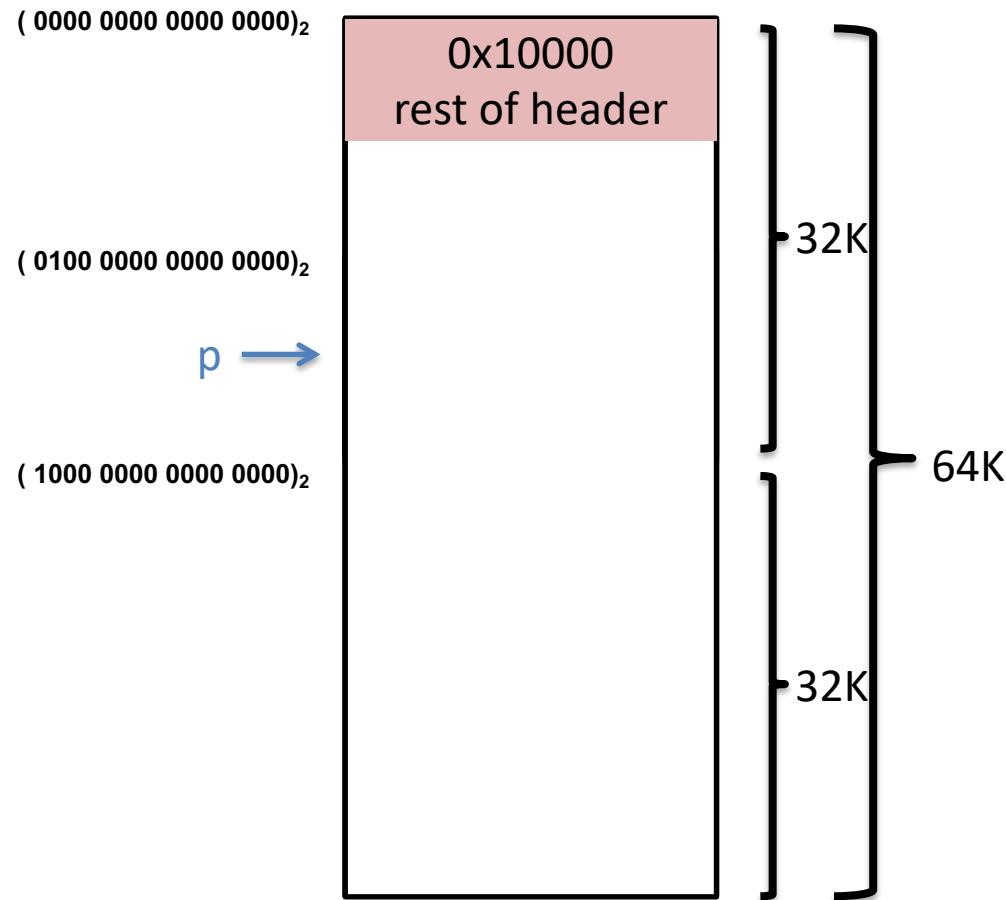
2. Detach free buddy from its list
3. Combine with current block



# Binary buddy system: free

free(p);

Repeat to merge with larger buddy  
Insert final block into appropriate  
freelist



# Summary

- Dynamic memory allocation
- Design constraints:
  - Free API does not include size
  - Space cannot be moved around
- Evolution of designs
  - Implicit list
  - Explicit list
  - Segregated list
  - Buddy system