Sequential Logic

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What we've learnt so far

- Combinatorial logic
  - E.g. Multiplexors (Mux), Decoders
  - Two ways of building a CL
    - Truth table → sum of products circuits
    - ROM
- ALU
  - Compute all operations (+, OR, AND, NOR), multiplexer picks the result
  - Building a 64-bit adder
    - Ripple carry chains together 1-bit adders
    - Carry lookahead

Today’s lesson plan

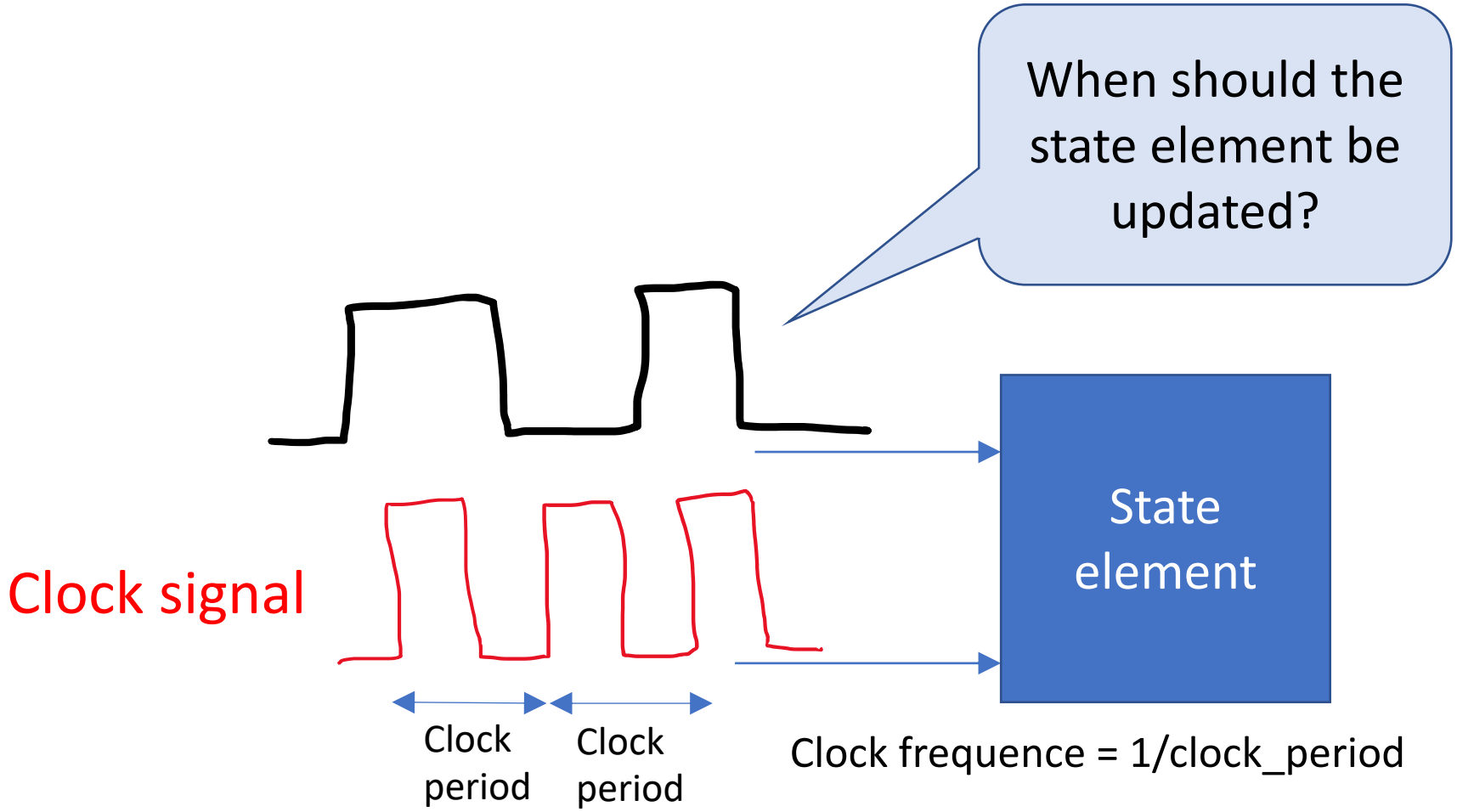
- Sequential circuit: Memory (state) elements
- Sequential circuit: Finite State Machine

Two types of logic circuits

- Combinatorial circuit
  - PLA: Truth table → sum of products PLA circuit
  - ROM (read-only memory): Addresses (inputs)→ contents (outputs)
- Sequential circuit
  - output is dependent on both input and state (memory elements)

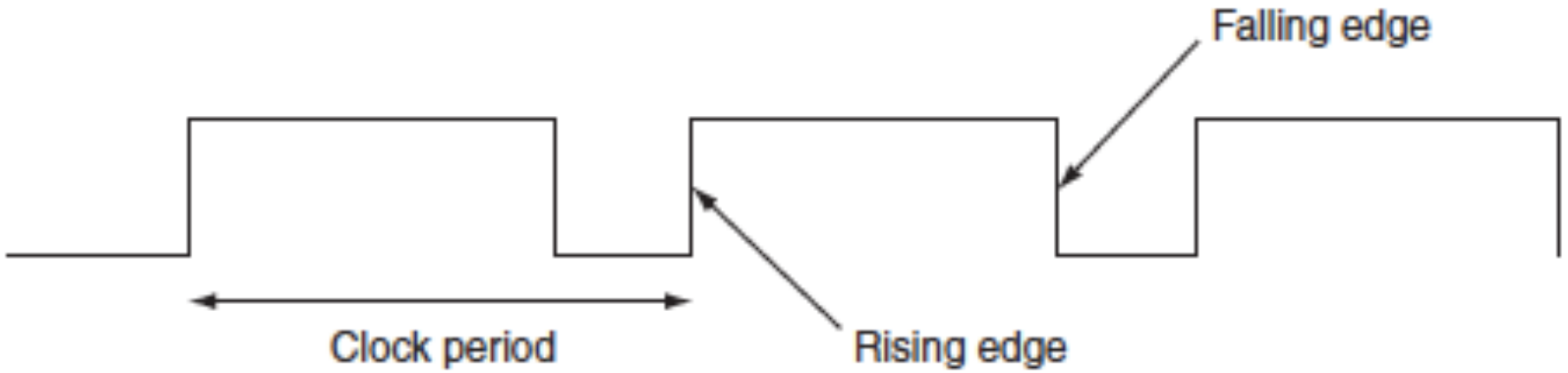
Today's lesson

Sequential logic requires clock

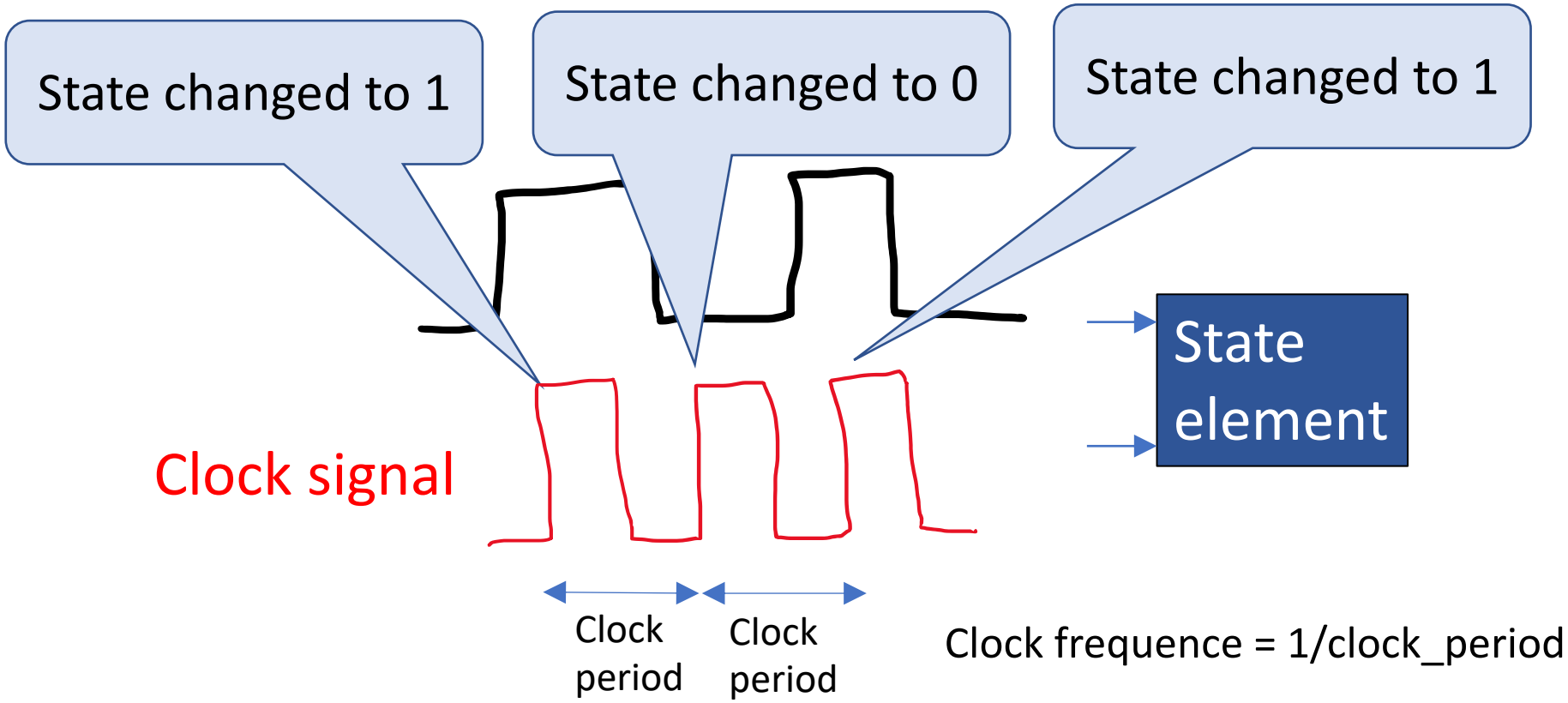


Clocks

- Edge-triggered clocking: state content only changes on active clock edge

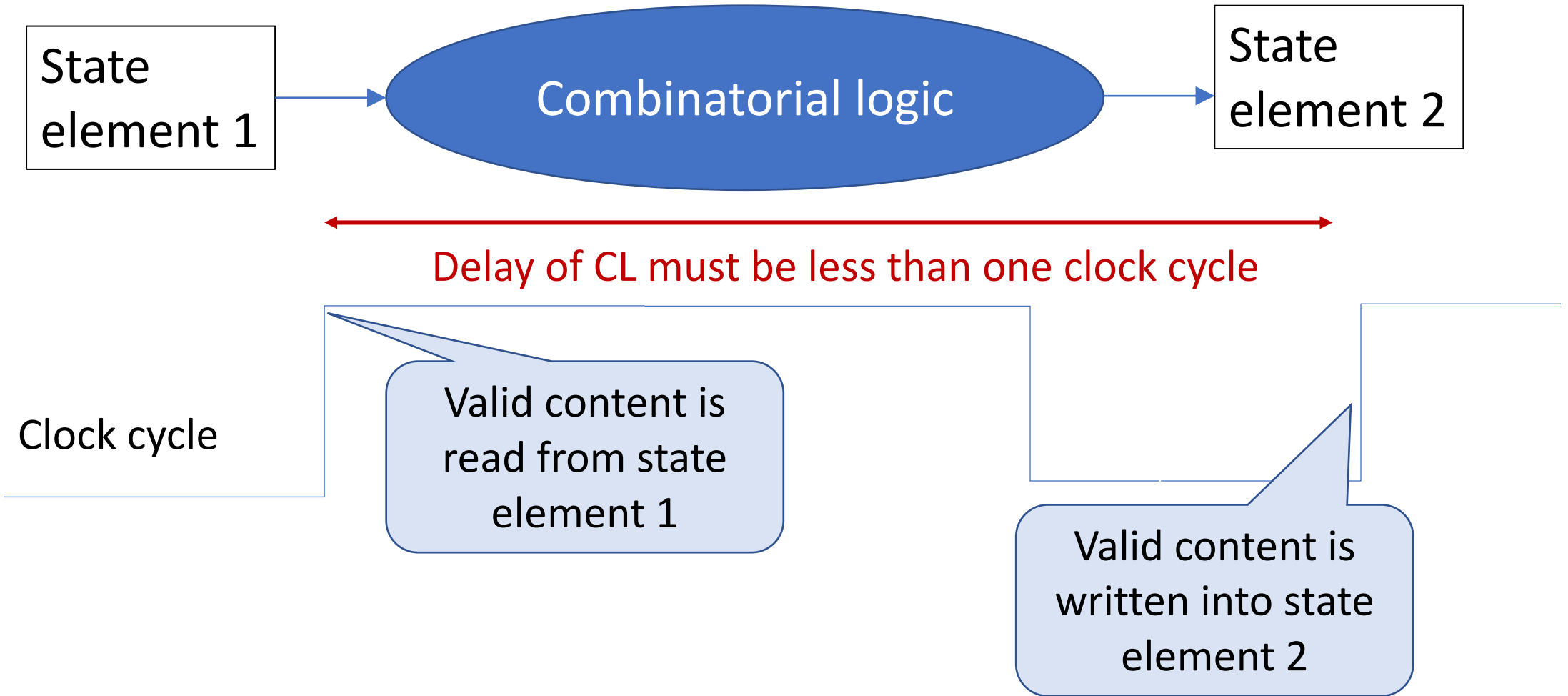


Sequential logic requires clock

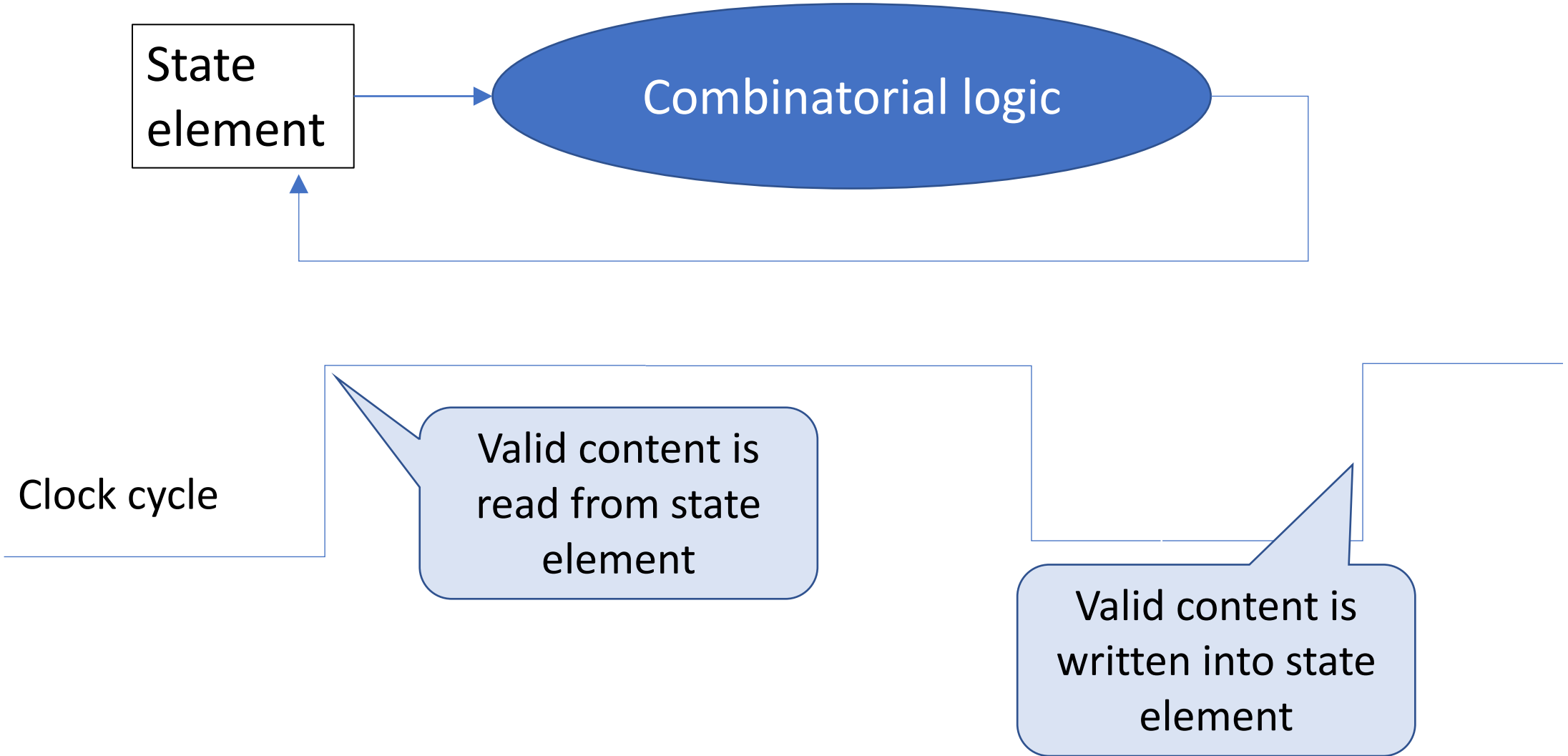


Clock frequence = 1/clock_period

Sequential logic requires clock

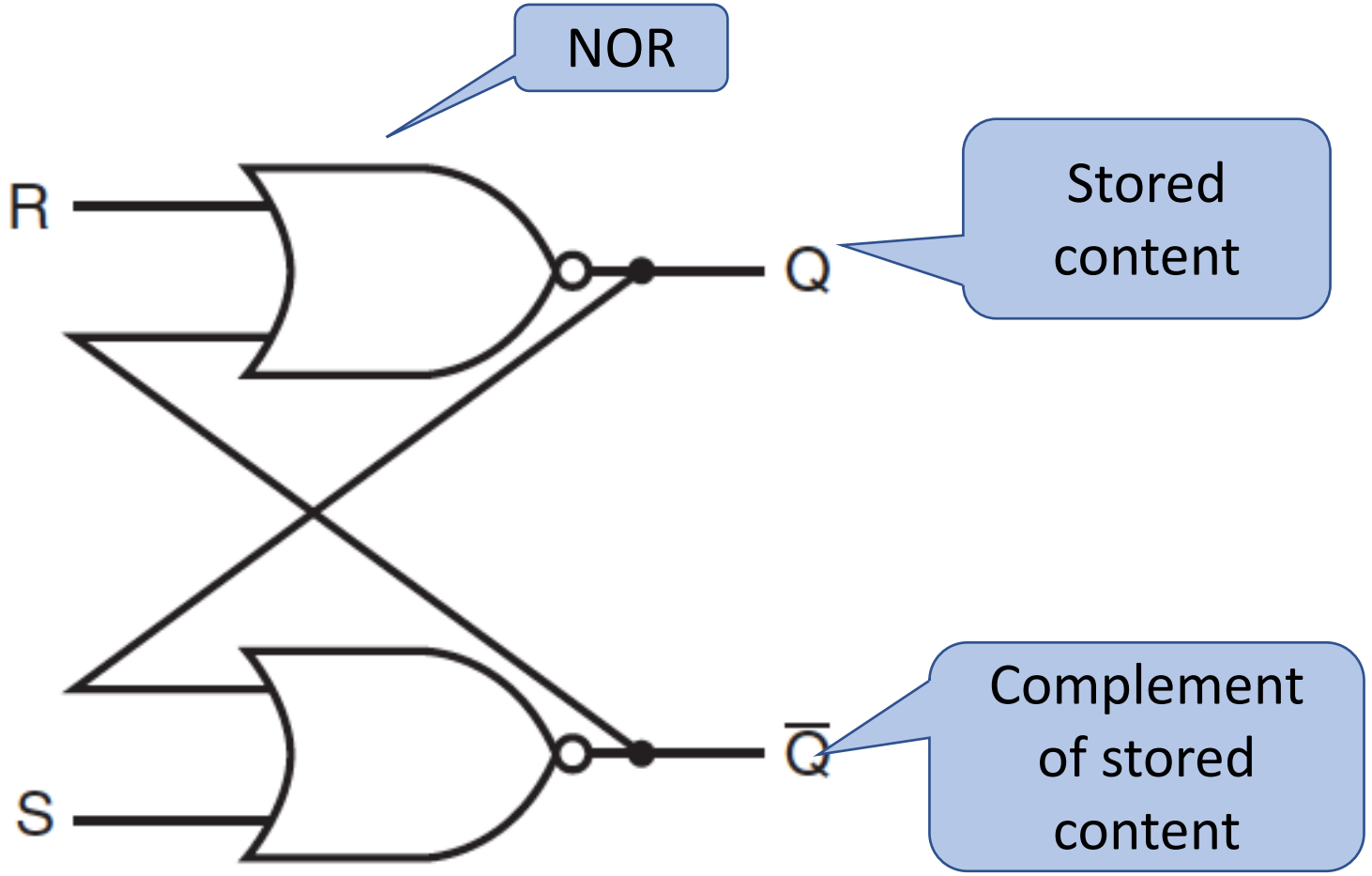


Sequential logic requires clock



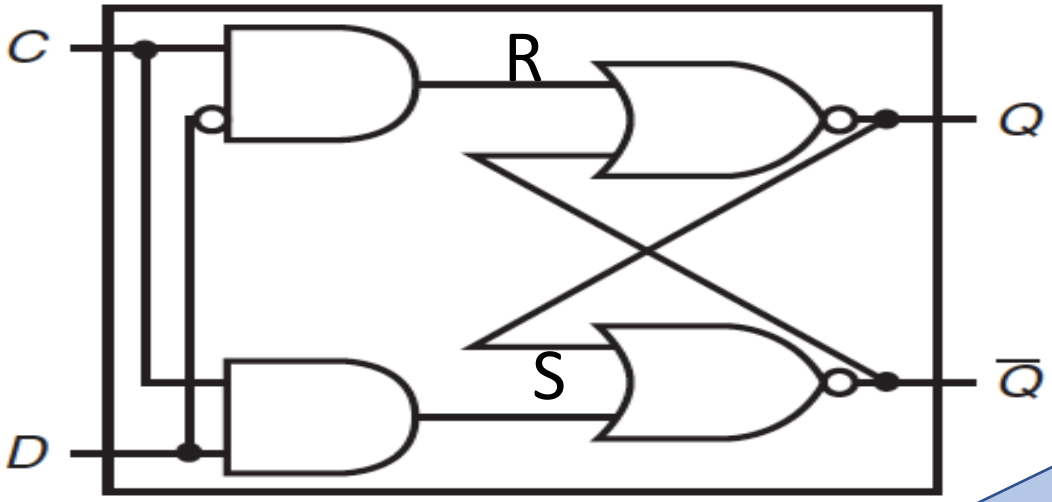
Memory (state) elements: unlocked S-R Latch

S (set)	R (reset)	
0	0	
1	0	
0	1	
1	1	



Memory element: clocked D latch

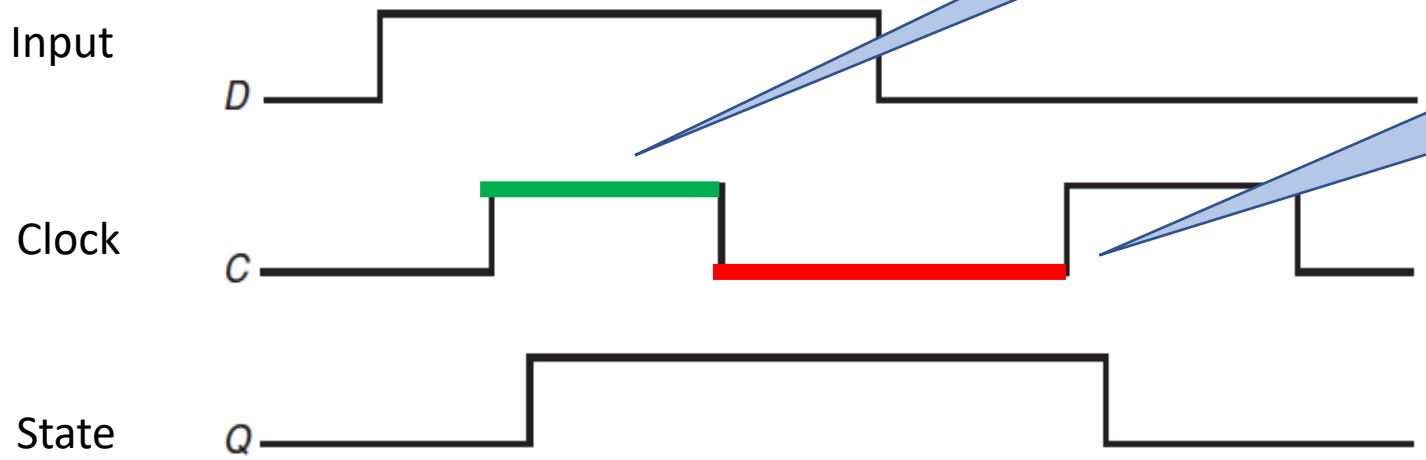
- D latch: state is changed as long as clock is asserted



Clock signal

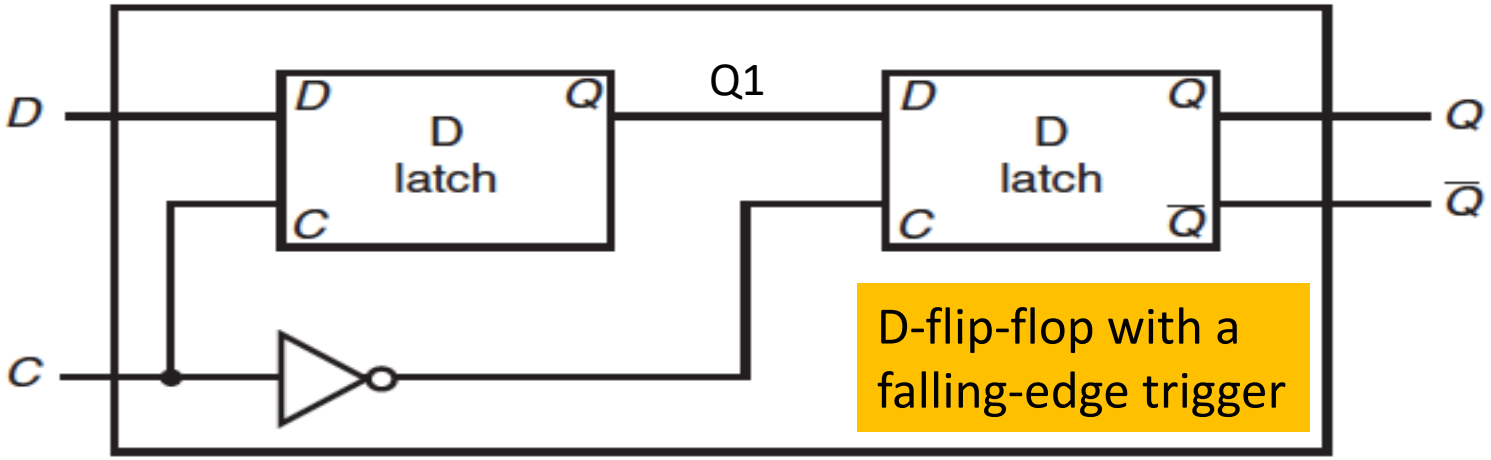
Latch is open; input is written to state

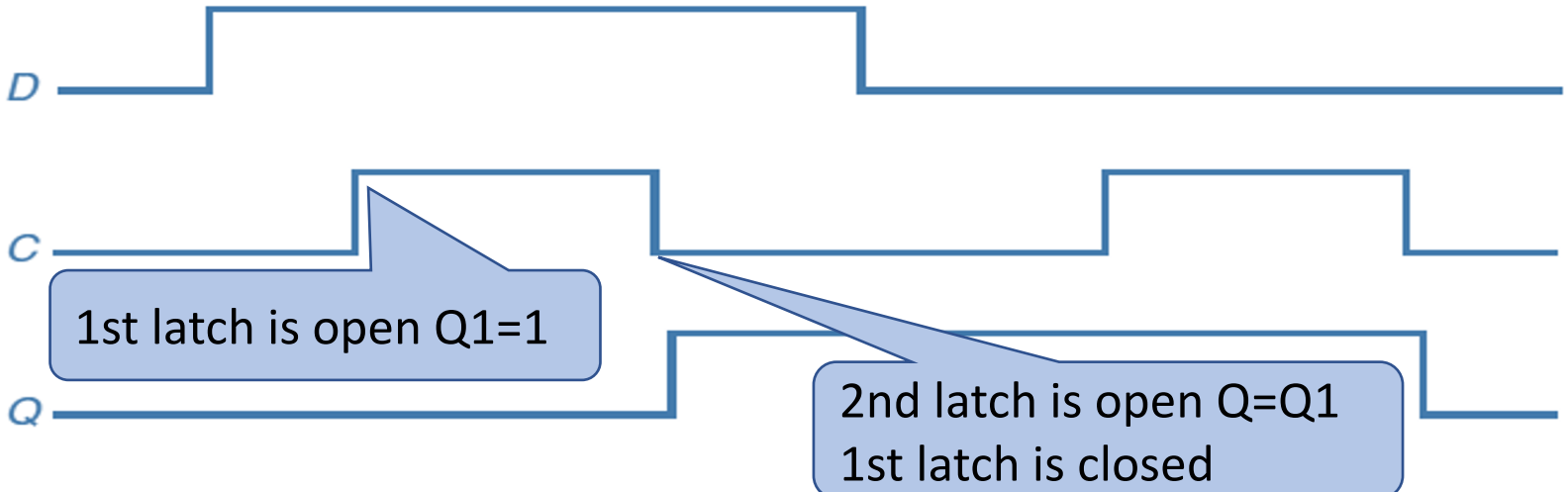
Latch is closed; state remains unchanged



Memory element: Flip-flop

- Flip-flop: state is changed only on (rising or falling) clock edge

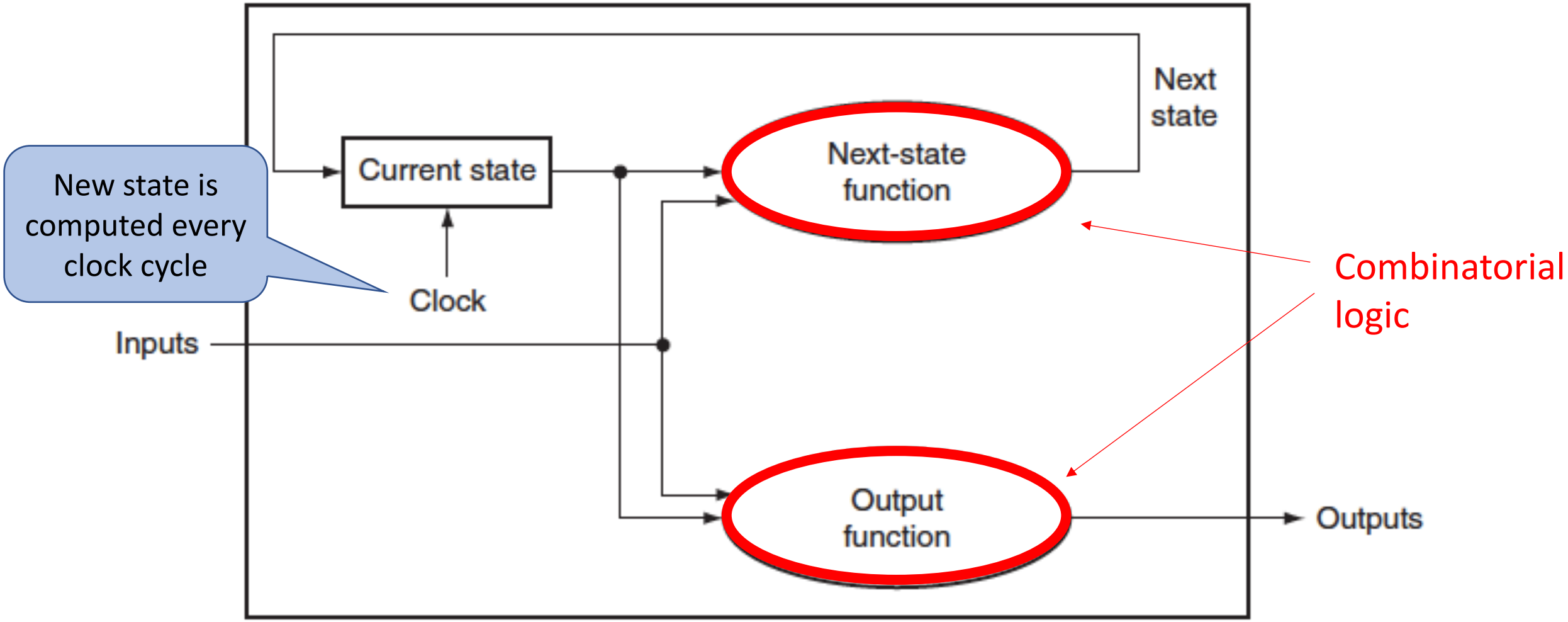




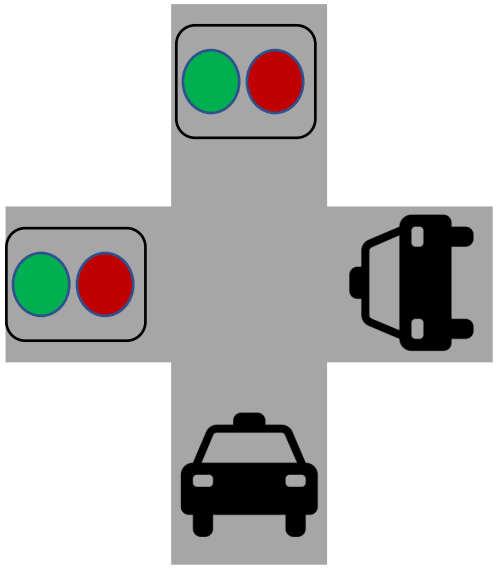
Finite State Machine

- Combinatorial logic → truth table
- Sequential logic → F(inite) S(tate) M(achine)
  - Input and current state determine next state and outputs

Finite State Machine



FSM example: traffic light control



How many bits needed to represent state values?

State:

NSgreen: traffic light is green in N-S (red in E-W)

EWgreen: traffic light is green in E-W (red in N-S)

Inputs:

NScar: car detected in N-S

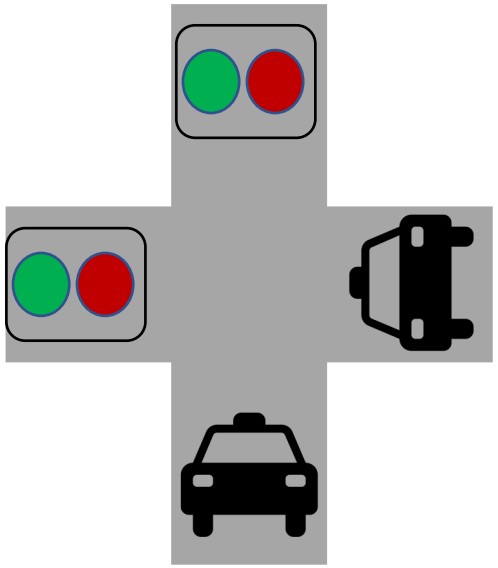
EWcar: car detected in E-W

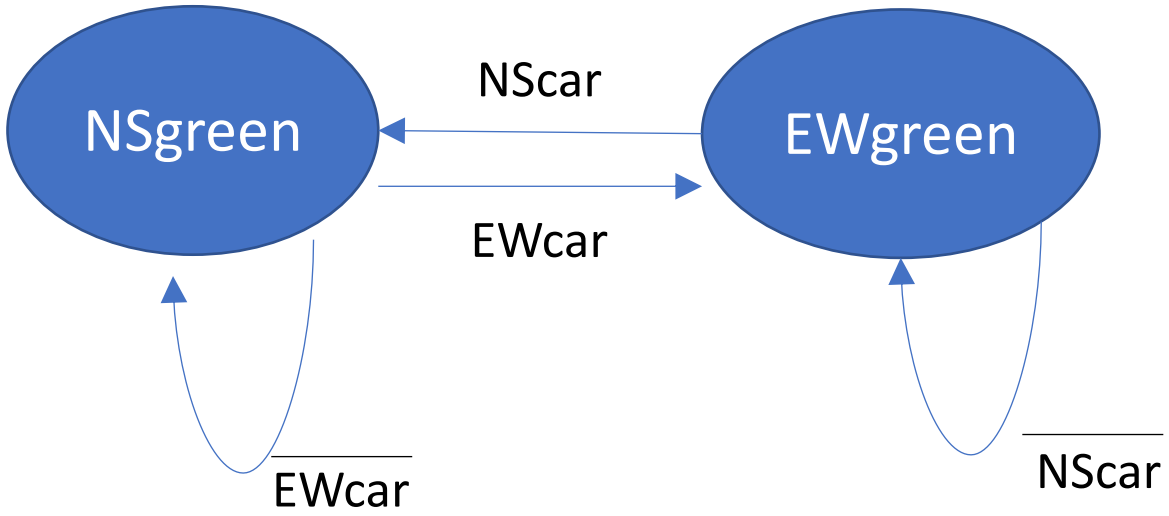
Outputs:

NSlite: 1 if state=NSgreen

EWlite: 1 if state=EWgreen

FSM example: traffic light control



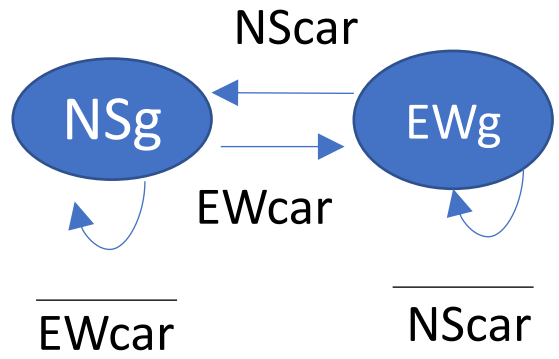


Clock speed? Clock cycles once every 30 seconds

FSM example: traffic light

- FSM is determined by NextState function and Output function

	Inputs		
	NScar	EWcar	Next state
NSgreen	0	0	NSgreen
NSgreen	0	1	EWgreen
NSgreen	1	0	NSgreen
NSgreen	1	1	EWgreen
EWgreen	0	0	EWgreen
EWgreen	0	1	EWgreen
EWgreen	1	0	NSgreen
EWgreen	1	1	NSgreen



FSM example: traffic light

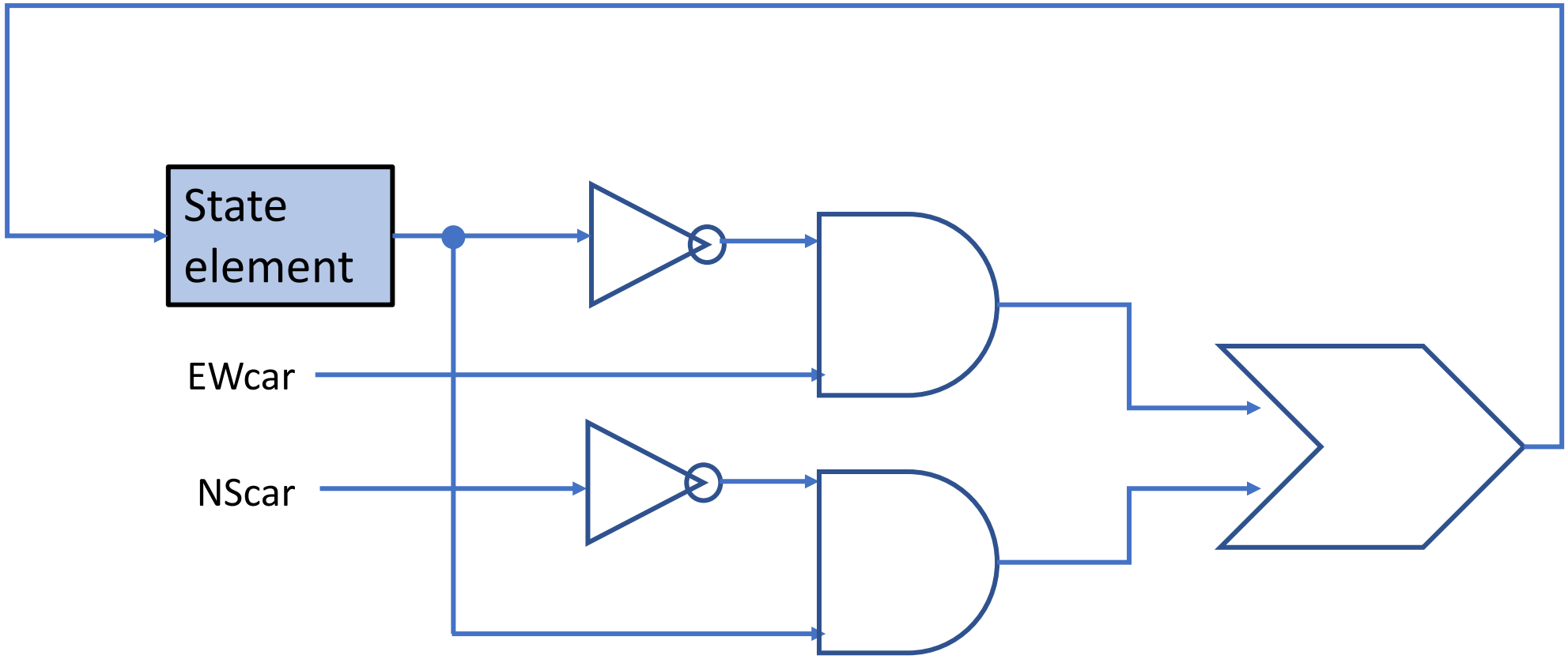
- FSM is determined by NextState function and Output function

Current State	Inputs		
	NScar	EWcar	Next state
0 (Nsgreen)	0	0	0 (Nsgreen)
0 (Nsgreen)	0	1	1 (Ewgreen)
0 (Nsgreen)	1	0	0 (Nsgreen)
0 (Nsgreen)	1	1	1 (Ewgreen)
1 (Ewgreen)	0	0	1 (Ewgreen)
1 (Ewgreen)	0	1	1 (Ewgreen)
1 (Ewgreen)	1	0	0 (Nsgreen)
1 (Ewgreen)	1	1	0 (Nsgreen)

$$Next = \overline{Curr} \cdot \overline{NScar} \cdot EWcar + \overline{Curr} \cdot NScar \cdot EWcar + Curr \cdot \overline{NScar} \cdot \overline{EWcar} + Curr \cdot \overline{NScar} \cdot EWCar$$

FSM traffic light: next state function

$$Next = \overline{Curr} \cdot EWcar + Curr \cdot \overline{NScar}$$



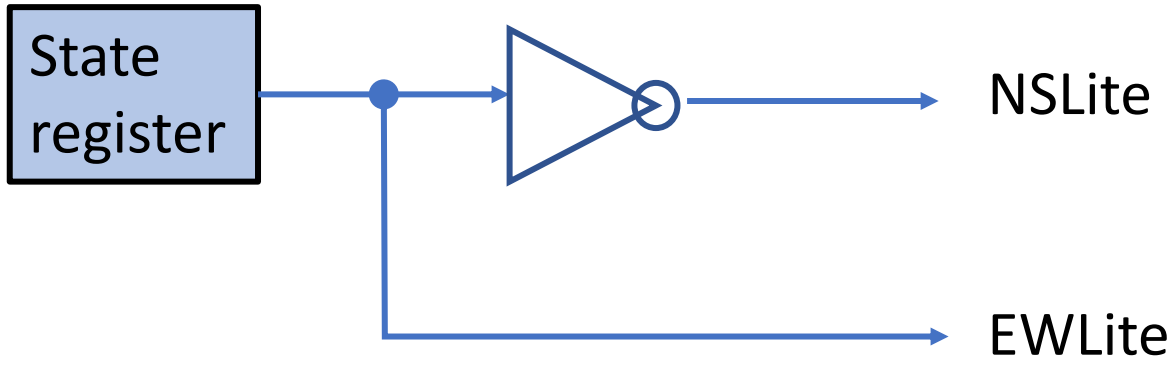
FSM traffic light: output function

		Outputs	
		NSlite	EWlite
0	NSgreen	1	0
1	EWgreen	0	1

NSLite $= \overline{Curr}$

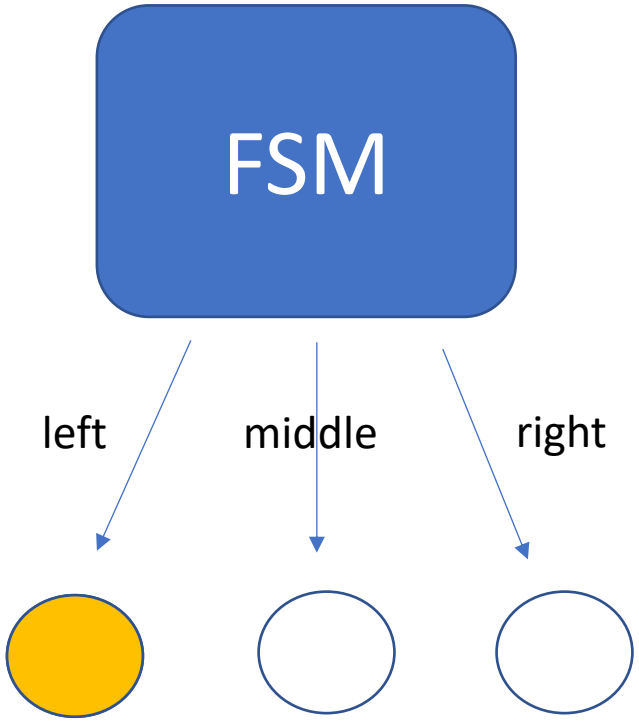
EWLite = $Curr$

FSM traffic light: output function



Another FSM example: Electronic eye

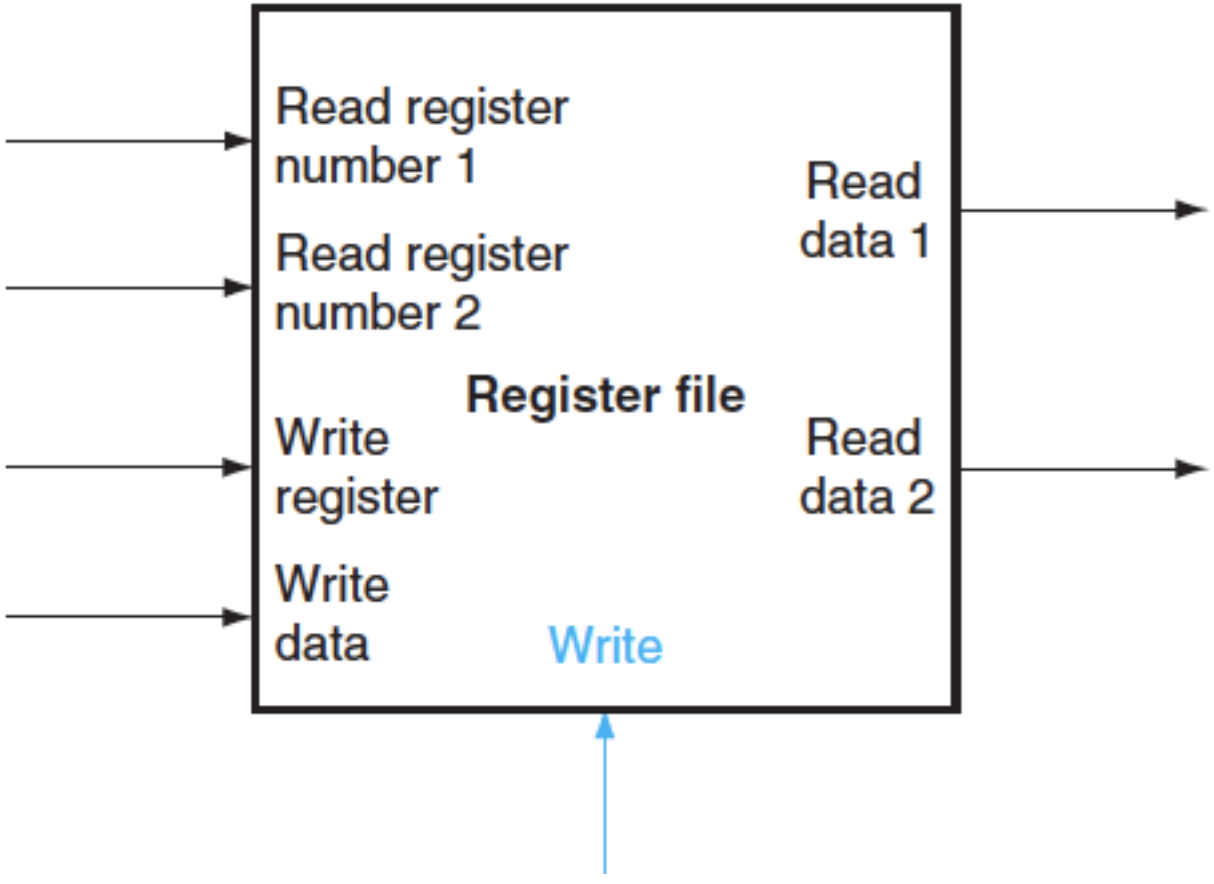
State transition diagram?



Lights are lit from left to right, then right to left and so on

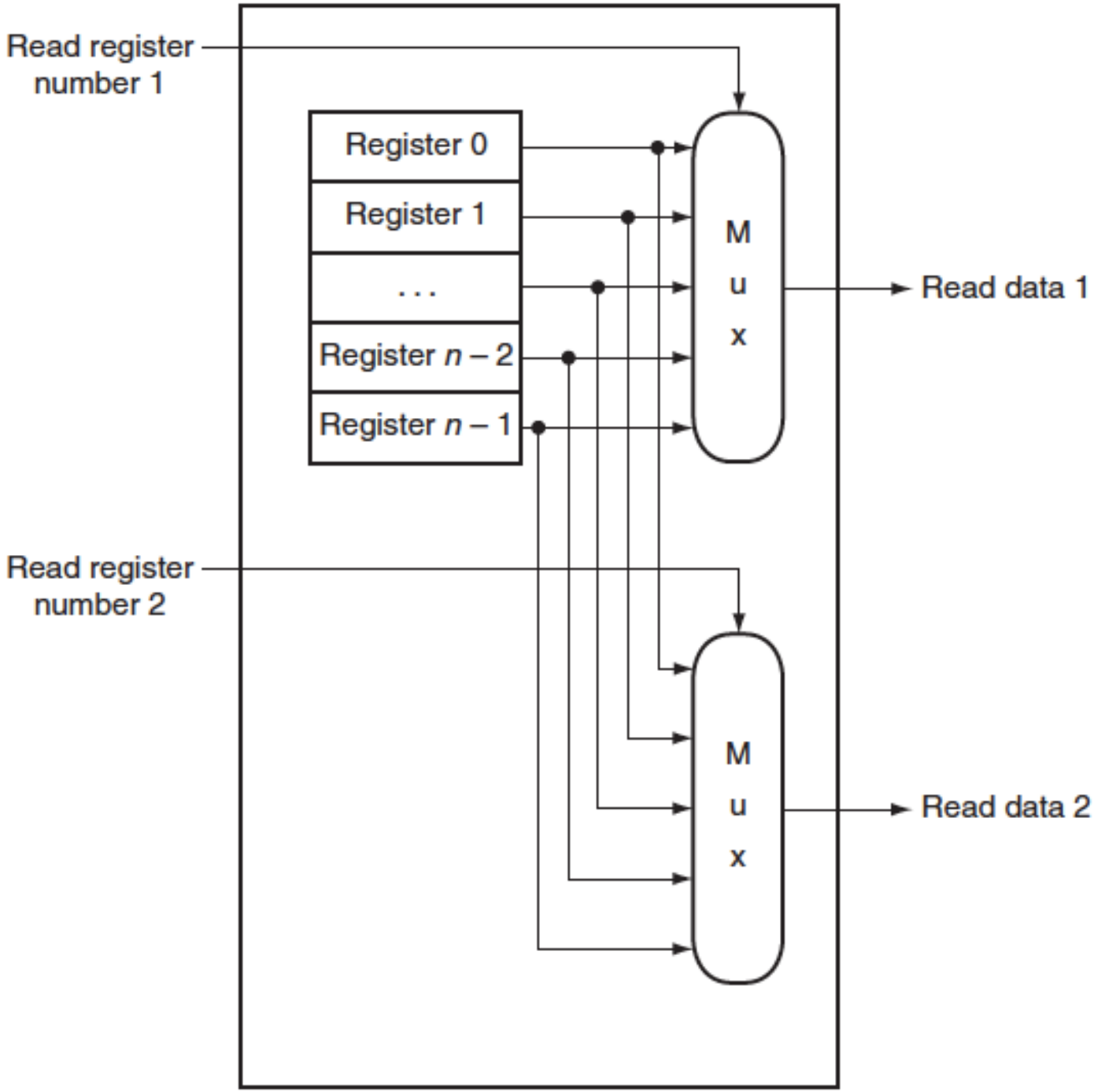
Memory element: Register file

- Register file: a set of registers that can be read and written



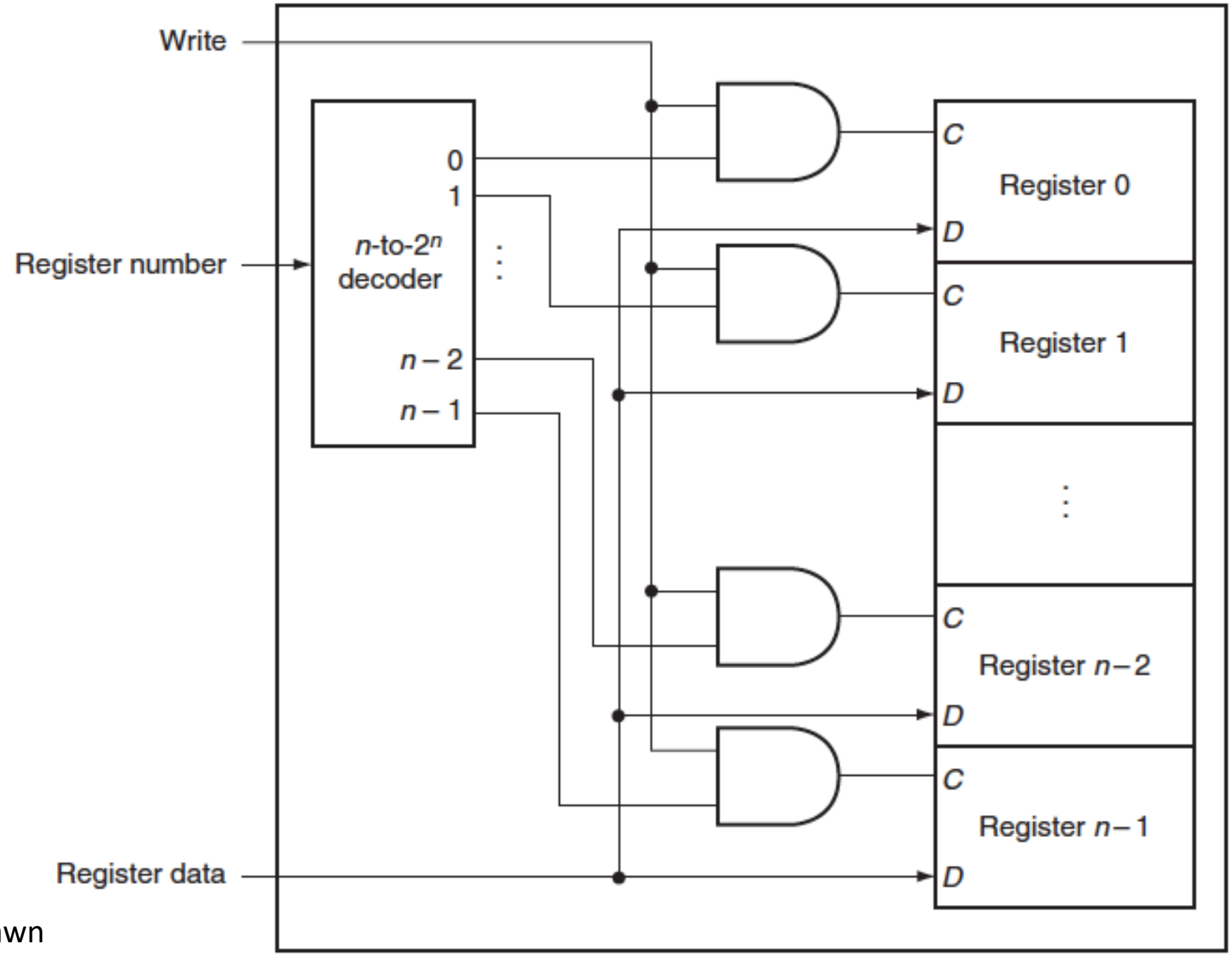
😕Why reading two registers at a time?

Register file: Read



Clock signal is assumed and not drawn

Register file: Write



Clock signal is assumed and not drawn

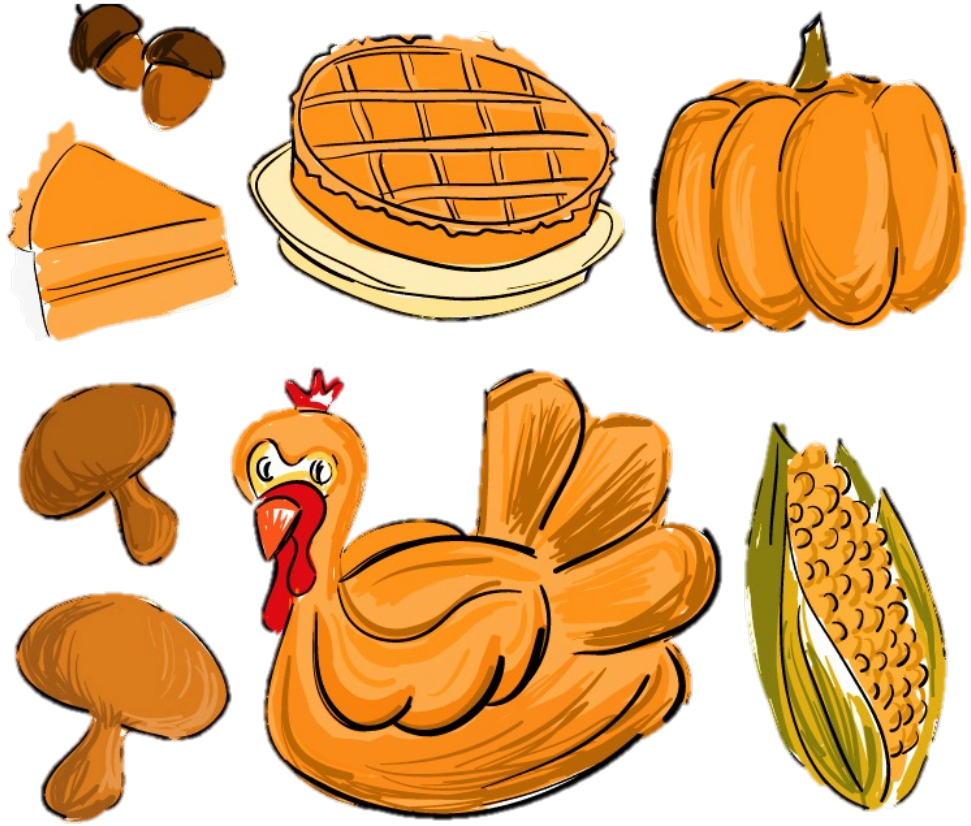
Register file

- What if the same register is read and written in the same clock cycle?
  - Return register value written in an earlier cycle
  - Write of new value occurs on the clock edge (at the end of the current cycle)
- Some register file can read value currently being written
  - Requires additional logic in the register file

Summary

- Memory (state) elements
  - Requires a clock signal to know when to update state value
  - Unclocked S-R latch → Clocked D latch → Flip-flop
- Sequential logic
  - Finite state machine
  - Decompose into two CL functions
    - Next state function: compute next state value based on current state value and inputs
    - Output function: compute output based on current state value and inputs

Happy Thanksgiving!



Stay safe!